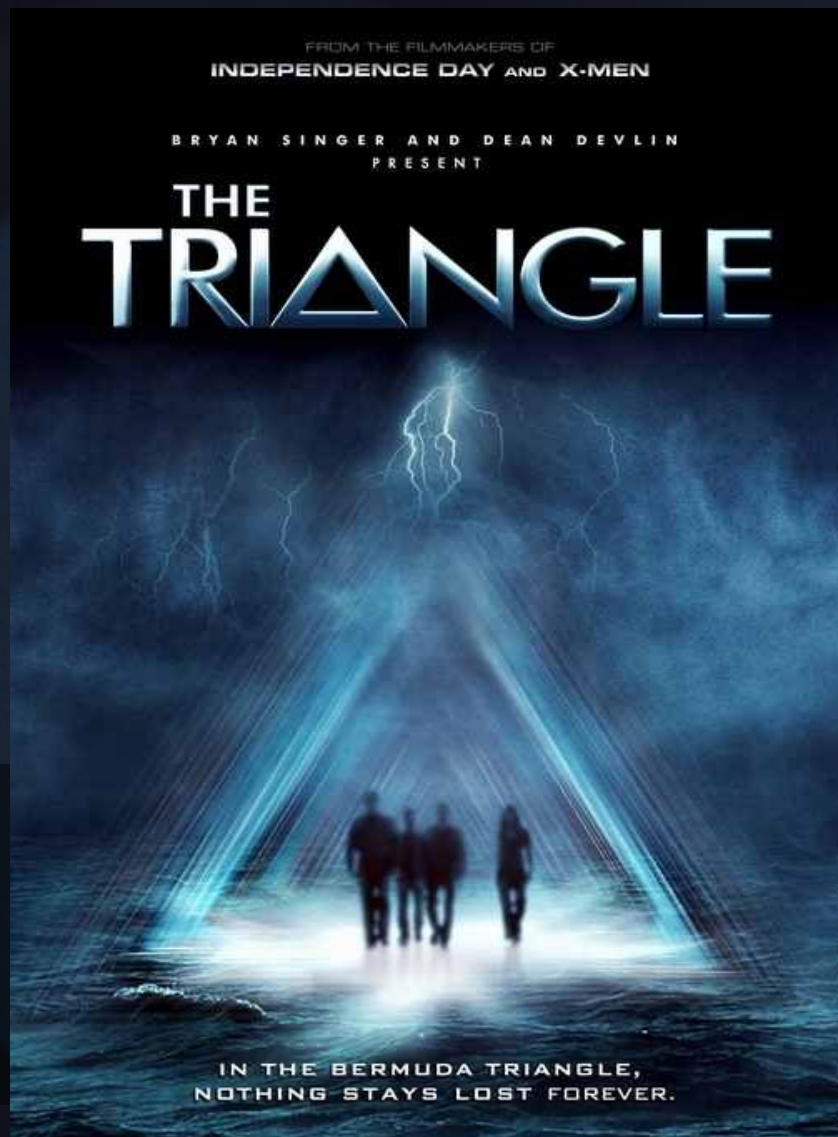


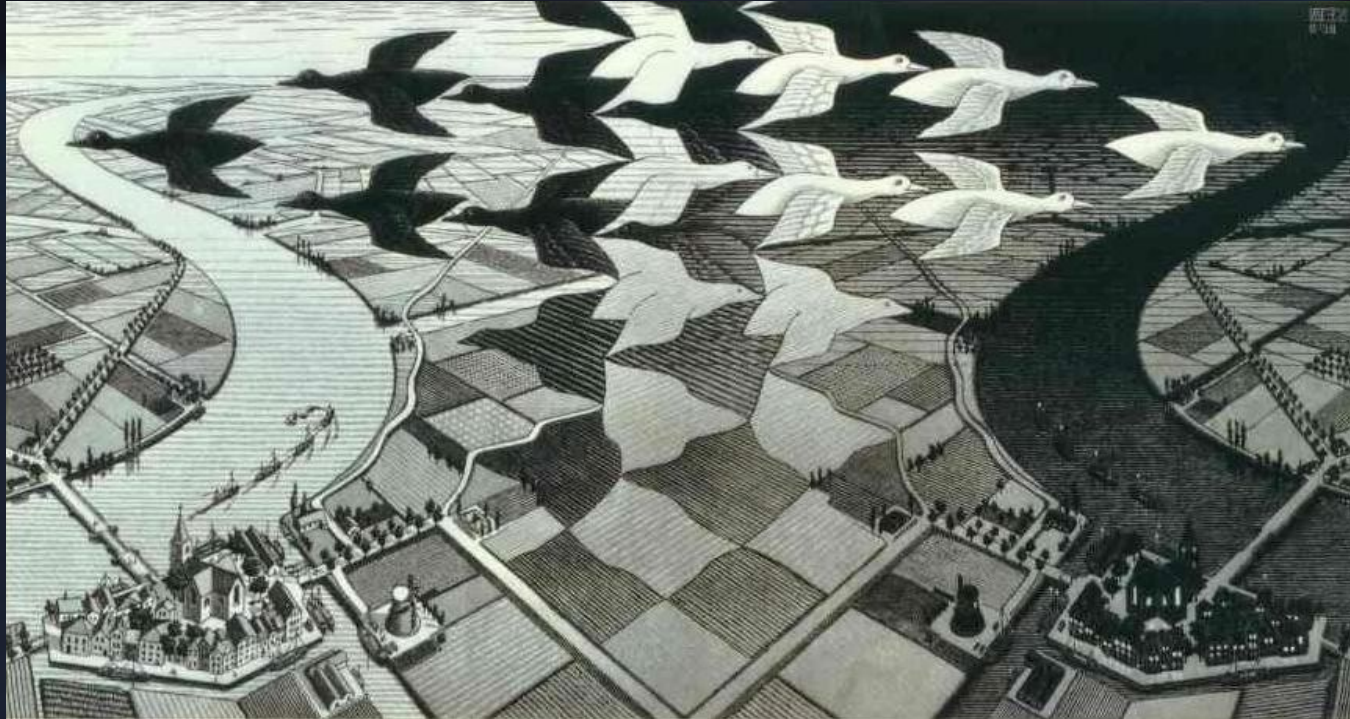


HEP Theory Group Seminar  
December 26<sup>th</sup>, 2006,  
Department of Physics, CYCU

Kai-Feng Chen  
National Taiwan University

The Belle Collaboration

Measurements on  
CKM Angles  $\phi_1$ ,  $\phi_2$  &  $\phi_3$



# *CP* Violation in *B* Physics: A Brief Introduction



## NOTES ON THE OBSERVABILITY OF $CP$ VIOLATIONS IN $B$ DECAYS

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Received 16 June 1981

The time-dependent  
 $CP$ -violation on  $B$ -system  
was proposed 25 years ago.

We describe a general method of exposing  $CP$  violations in on-shell transitions of  $B$  mesons. Such  $CP$  asymmetries can reach values of the order of up to 10% within the Kobayashi–Maskawa model for plausible values of the model parameters. Our discussion focuses on those (mainly non-leptonic) decay modes which carry the promise of exhibiting clean and relatively large  $CP$  asymmetries at the expense of a reduction in counting rates. Accordingly we address the complexities encountered when performing  $CP$  tests with a high statistics  $B$  meson factory like the  $Z^0$  (and a toponium) resonance.

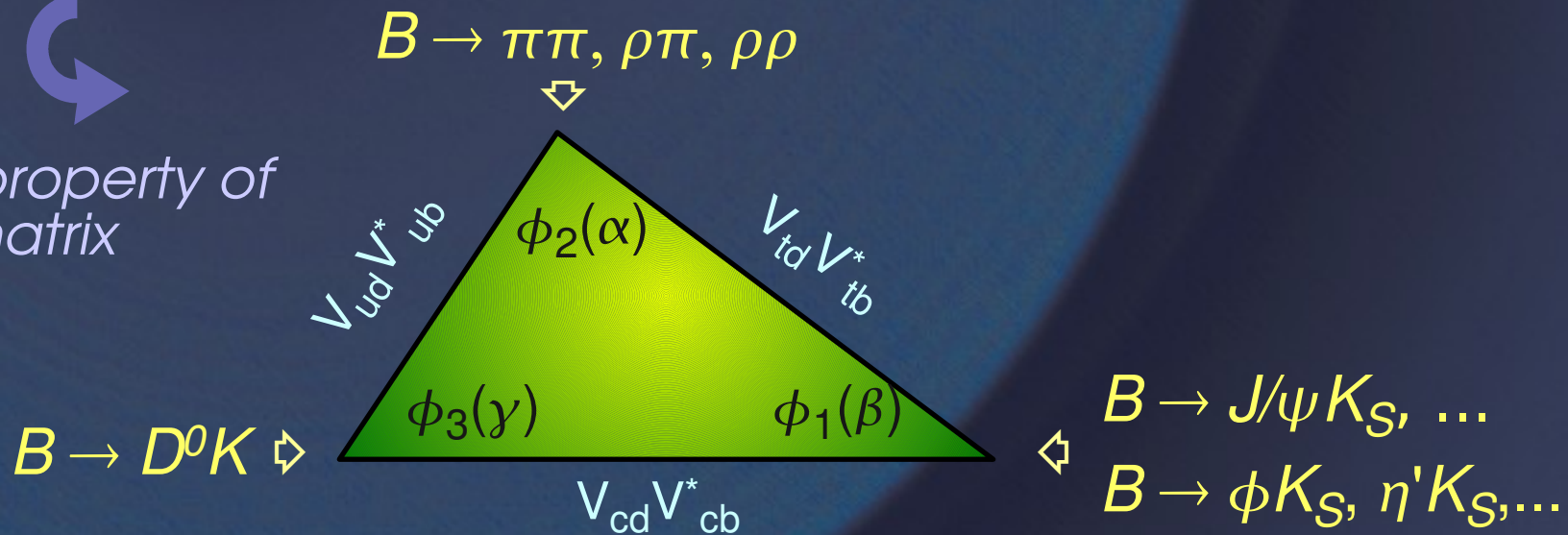
# ~~CP~~ in the Standard Model

$CP$  symmetry is broken by the complex phase appearing in the quark mixing matrix

$$\begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} = \begin{pmatrix} 1 - (\lambda^2/2) & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - (\lambda^2/2) & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$



Take the property of unitarity matrix

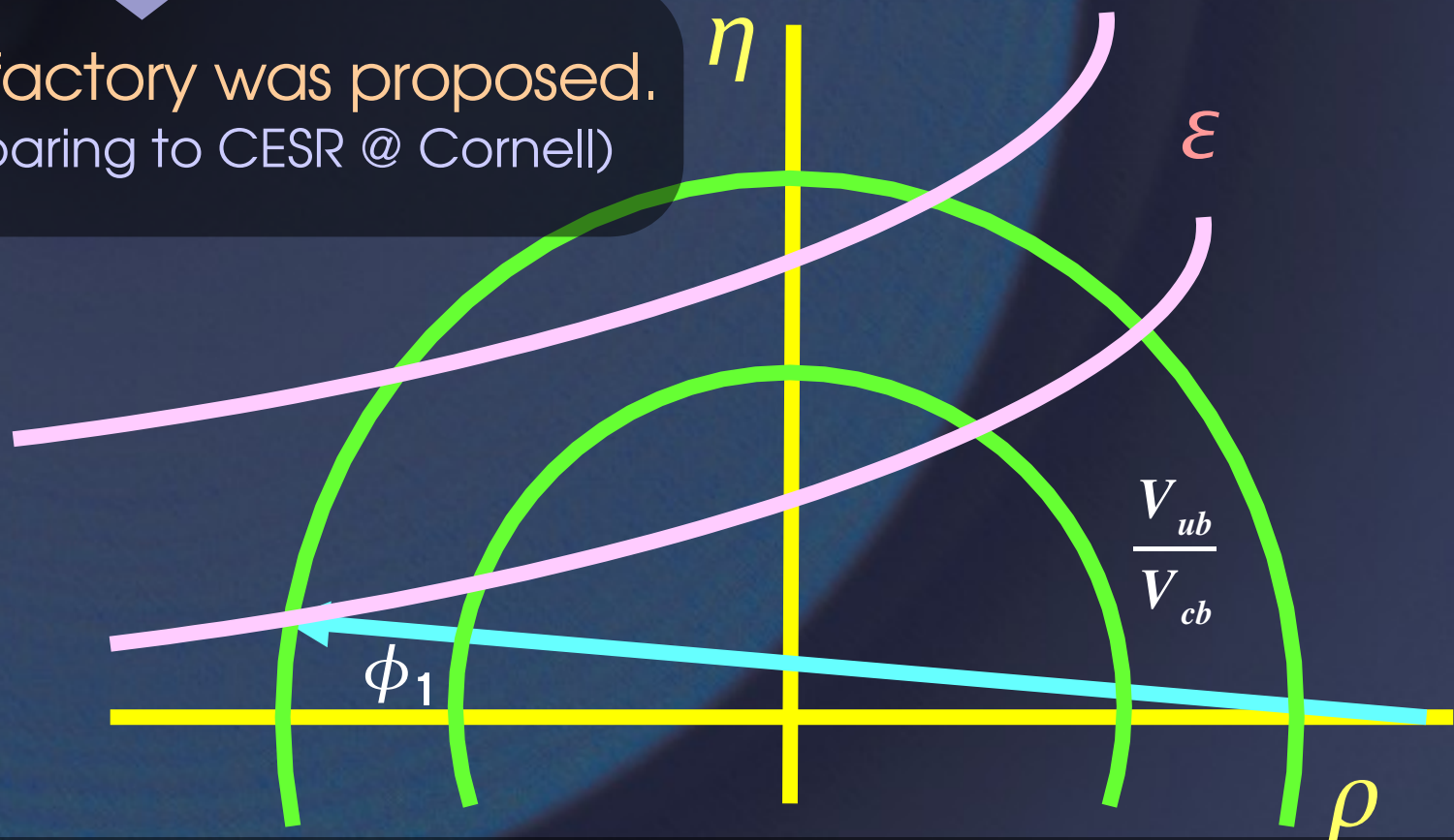




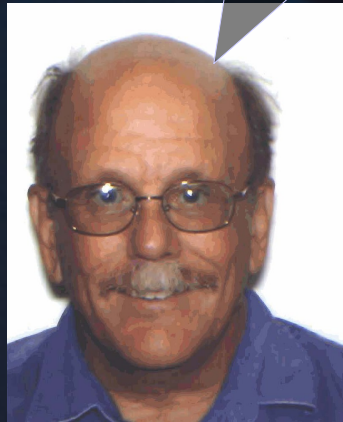
# Unitarity Triangle in 1980's

- ❑ The "known" minimum  $CP$  violation in  $B$  system is 15%.
- ❑ A lot of  $B$  mesons are required to measure the  $\phi_1$  angle.

A  $O(10^{34})$   $B$ -factory was proposed.  
(~1000x comparing to CESR @ Cornell)

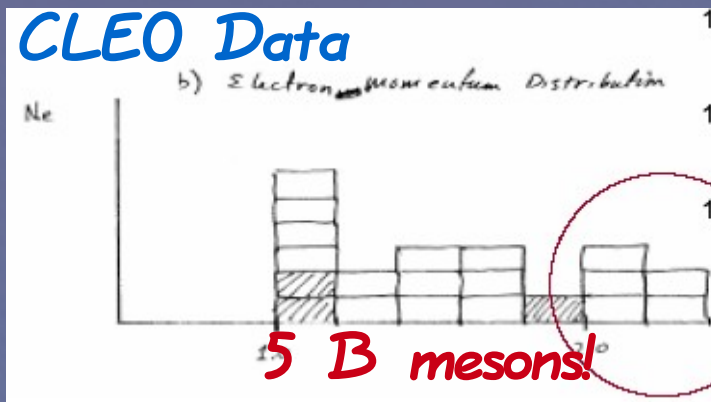


*Look! This took  
us six months!*



( $\Leftarrow$  S.Olsen)

*We need millions of  
 $B$  and use them to  
search for mixing and  
 $CP$  violation*



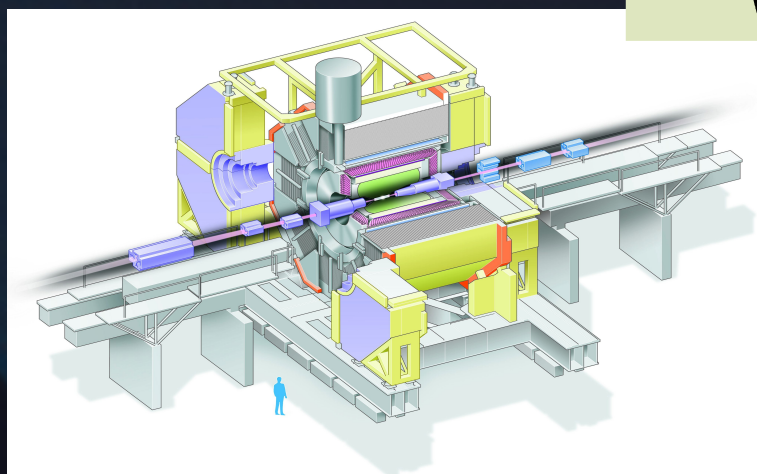


# B-Factory Experiments

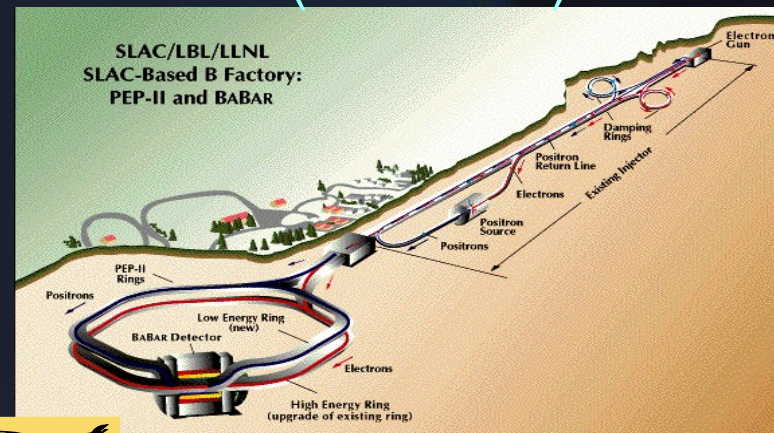
KEK(Japan)



Belle

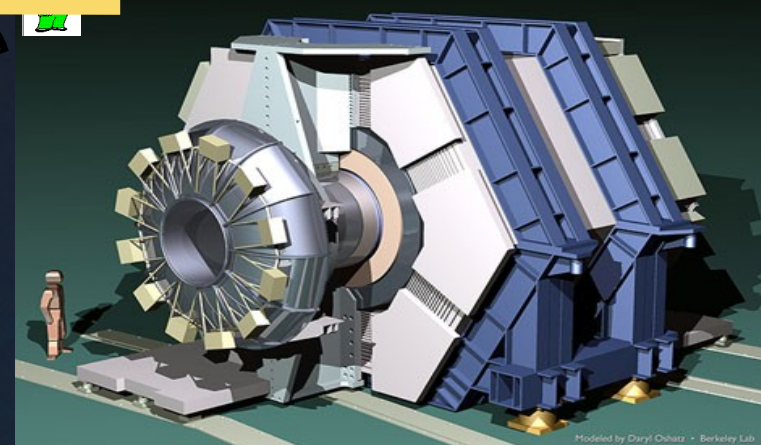


SLAC(Stanford)



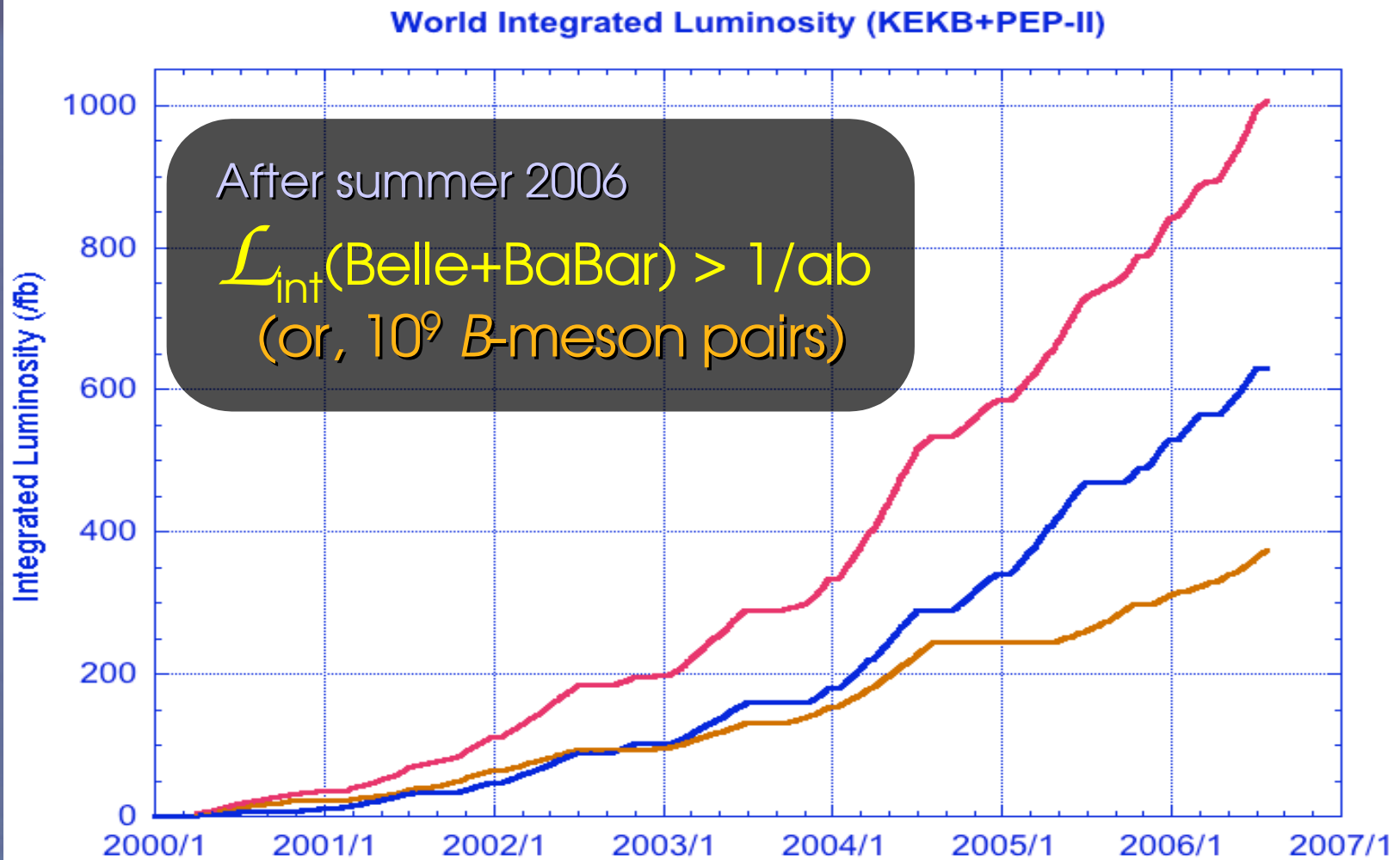
BaBar

BABAR DETECTOR FOR THE PEP-II B FACTORY





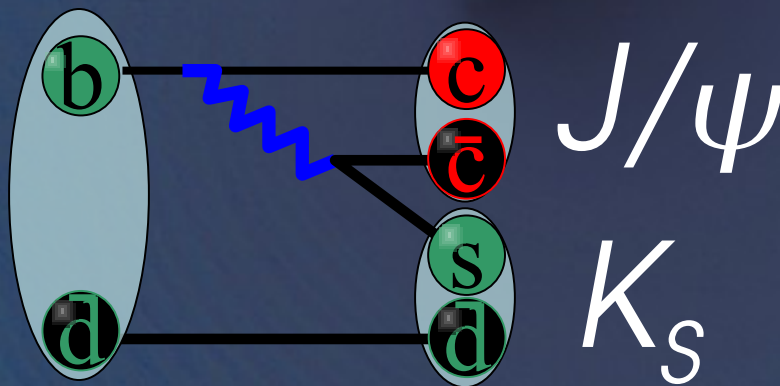
# Luminosity Records



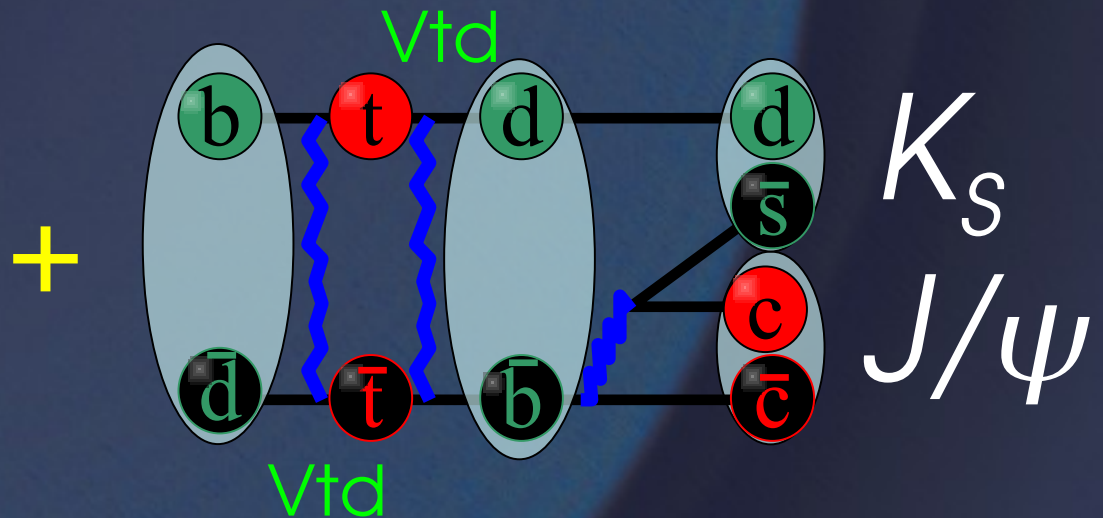
# Measurement of $\sin 2\phi_1$

Quantum Interference Between Two Diagrams:

Tree diagram



Box diagram + Tree diagram



We have to “wait” (i.e.  $\Delta t \neq 0$ ) to have contributions from the box diagram.



# Measurement of $\sin 2\phi_1$

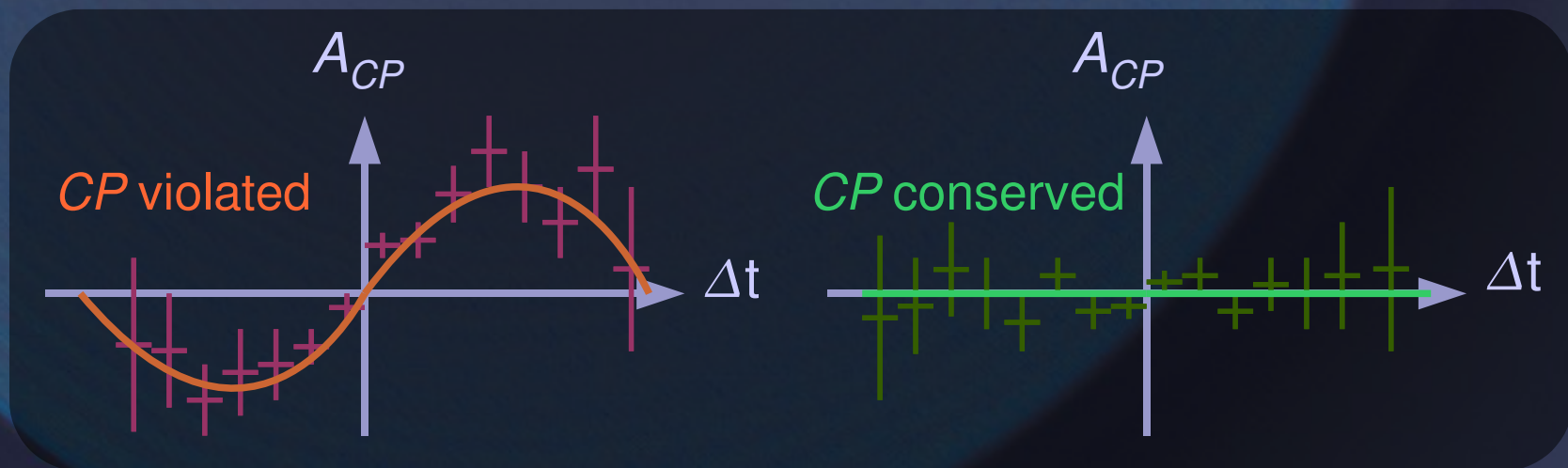
## Time-dependent $CP$ Asymmetries

$$A_{CP}(t) = \frac{\Gamma(\bar{B}^0 \rightarrow f_{CP}; t) - \Gamma(B^0 \rightarrow f_{CP}; t)}{\Gamma(\bar{B}^0 \rightarrow f_{CP}; t) + \Gamma(B^0 \rightarrow f_{CP}; t)} = \underbrace{A_f}_{\uparrow} \cos(\Delta m t) + \underbrace{S_f}_{\uparrow} \sin(\Delta m t)$$

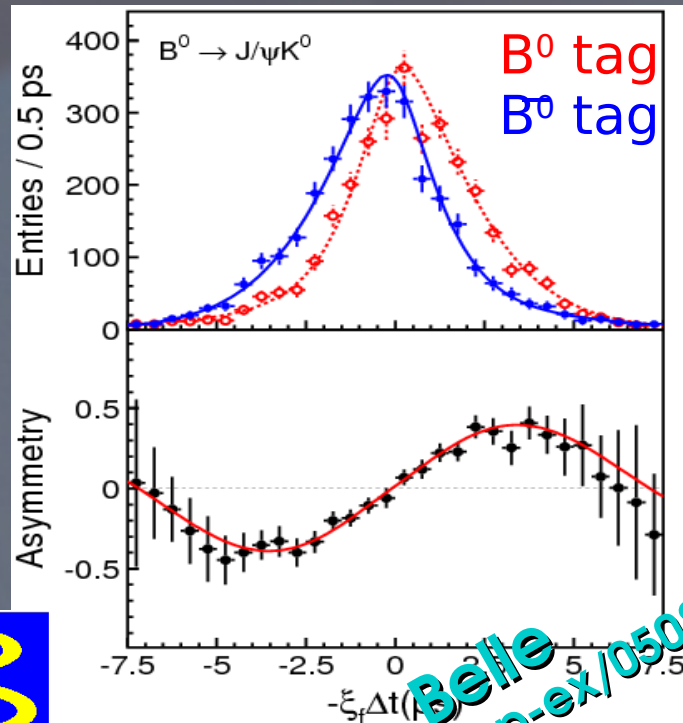
Indicates **direct  $CP$  violation**

$A_f = 0$  if  $f_{CP} = J/\psi K_S$   
 ( $-A_f = C_f$  in BaBar)

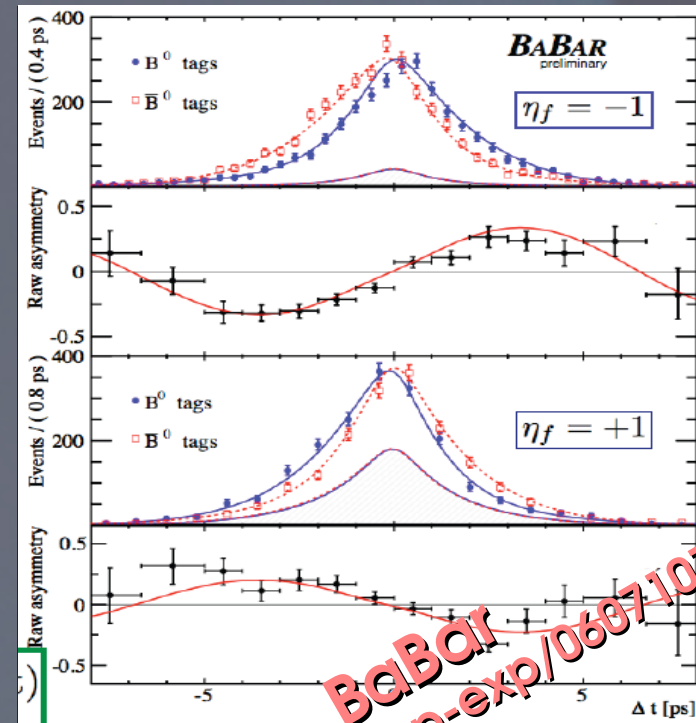
$S_f = \sin 2\phi_1$   
 if  $f_{CP} = J/\psi K_S$



# Measurement of $\sin 2\phi_1$



Belle  
hep-ex/0508039



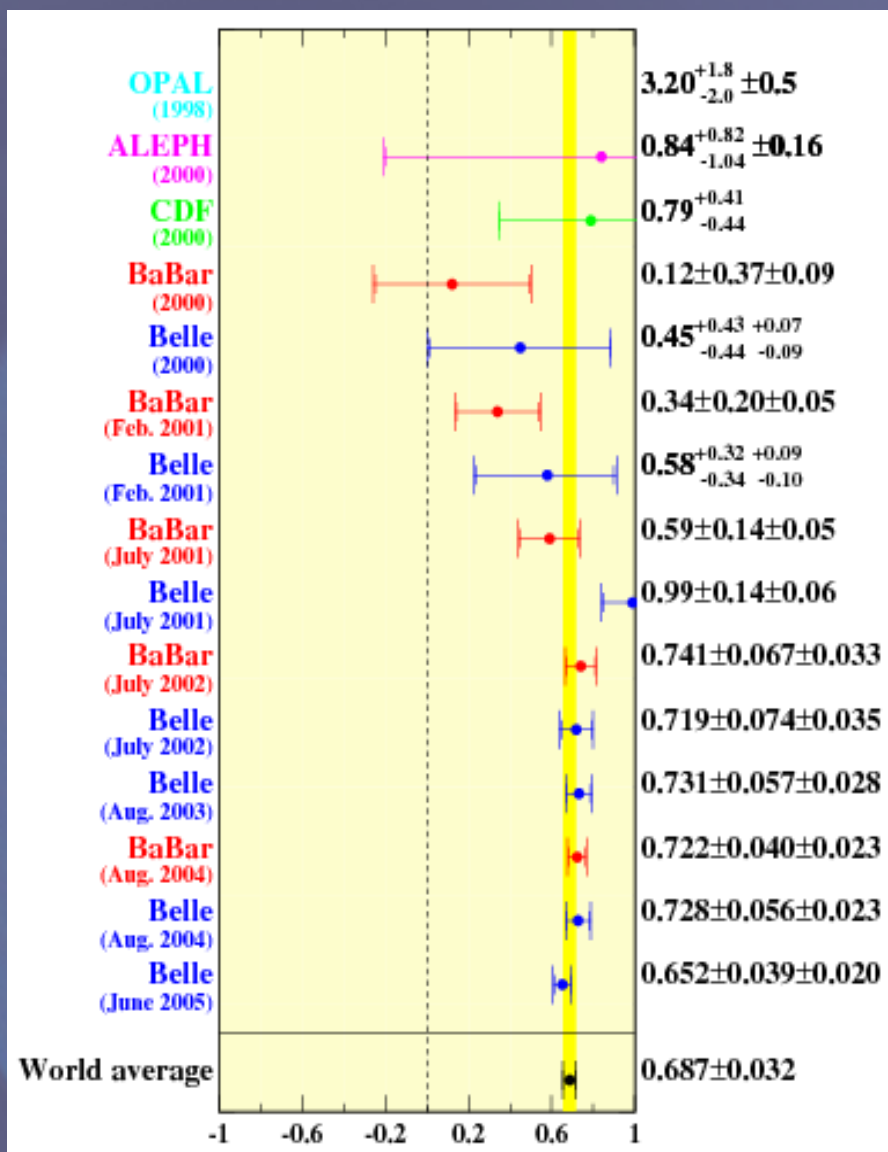
BaBar  
hep-ex/0607107



HFAG ( $b \rightarrow ccs$ ):  $S_{ccs} = 0.674 \pm 0.026$   
 ( $A_{ccs} = 0.012 \pm 0.022$ , consists of no  $DCPV$ )

$CP$  Violation in  $B$  system  
 is already established within  
 the Standard Model.

# Brief History (1998-2005) of $\sin 2\phi_1$ :



- Q: What is the main source of CP violation?
- A: The Kobayashi-Maskawa phase IS the dominate source!



- Q: Is there anything else?
- A: Not clear yet! Two approaches:
- 1) Over-constrain the unitary triangle with precise measurements on  $\phi_2/\phi_3$  as well.
  - 2) Compare  $\sin 2\phi_1$  in tree and penguin processes.





# The Experiment

(Mostly about the Belle Analysis)

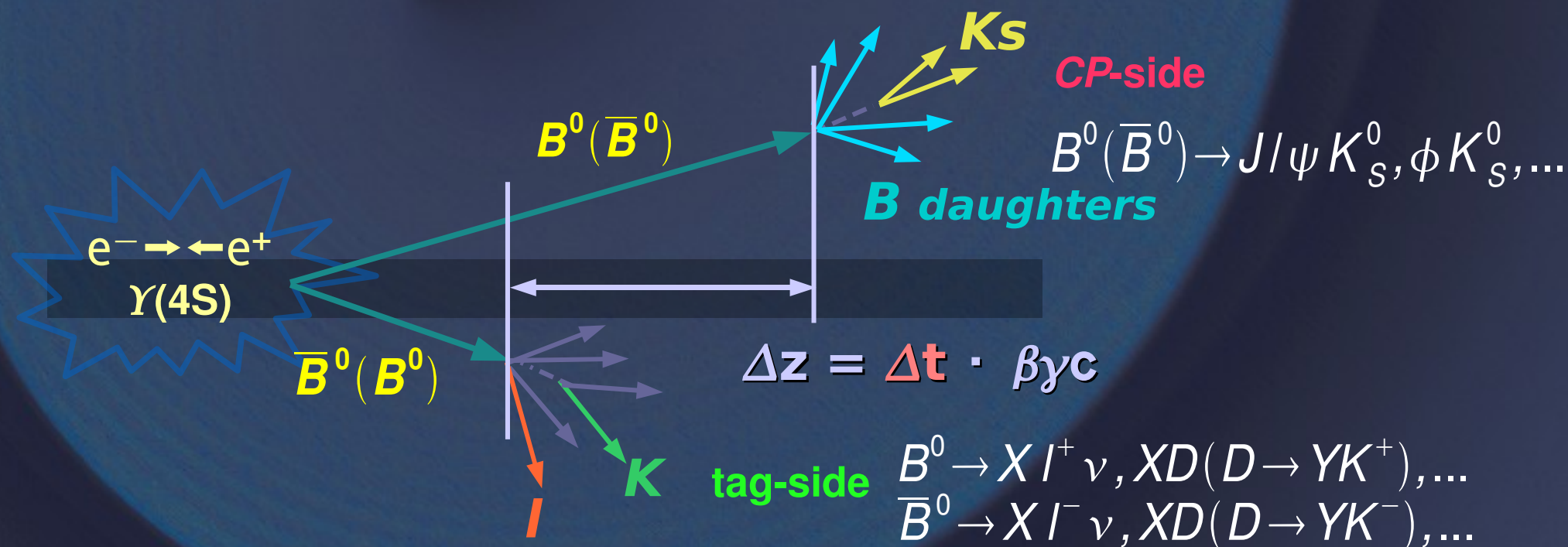
# The Measurements

- The experiments take the advantage of energy-asymmetric collider to produce Lorentz boosted  $B$  mesons.
- Fully reconstruct a  $CP$  eigenstate.
- Tags the  $B$  flavor from the associated  $B$  meson.
- Measures the proper-time difference ( $\Delta t$ ), and extract the  $CP$  asymmetries.

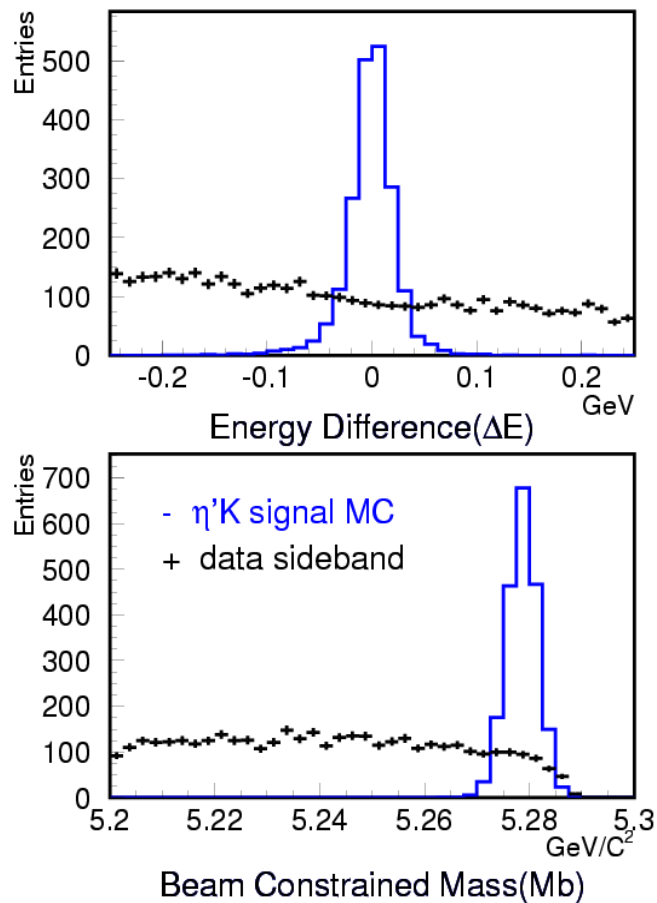
↗ Key point 1

↗ Key point 2

↗ Key point 3



# Event Reconstruction



- $B$  candidates are identified by the beam constrained mass ( $M_{bc}$ ), and the energy difference ( $\Delta E$ ):

$$\left[ \begin{aligned} M_{bc} &= \sqrt{E_{beam}^2 - P_B^2} \\ \Delta E &= E_B - E_{beam} \end{aligned} \right.$$

where  $E_B$  and  $P_B$  are the reconstructed  $B$  energy and momentum in the cms frame.

- Dominated background events are from continuum processes ( $e^+e^- \rightarrow q\bar{q}$ ).

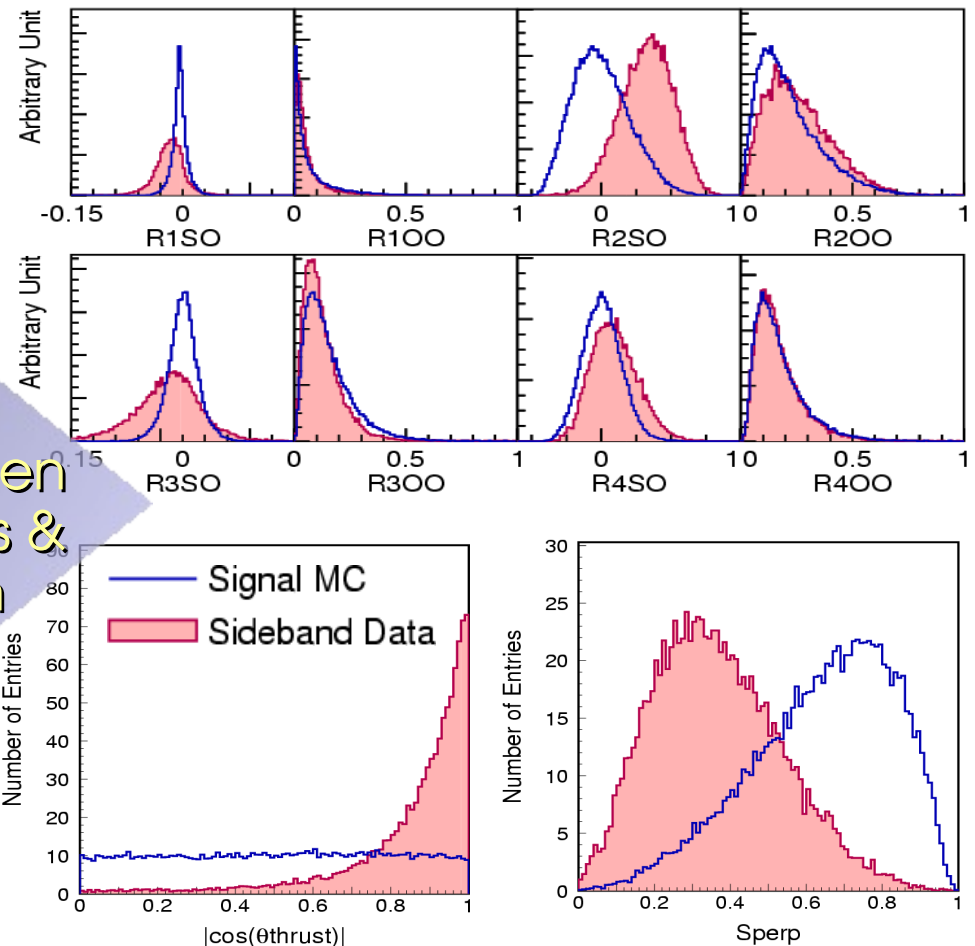


# Continuum Suppression

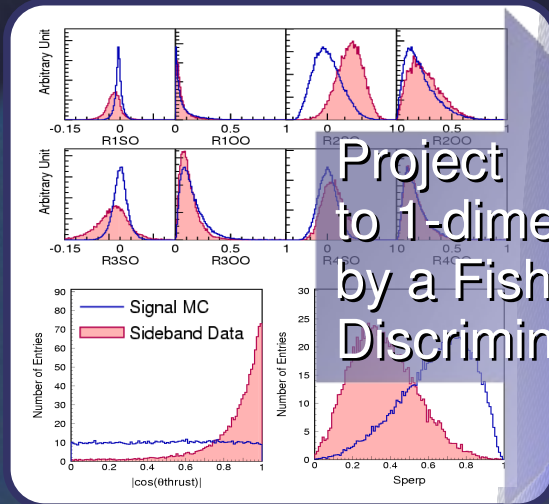
$B^0/\bar{B}^0$

Exploit the difference between spherical  $B$  events & jet-like continuum

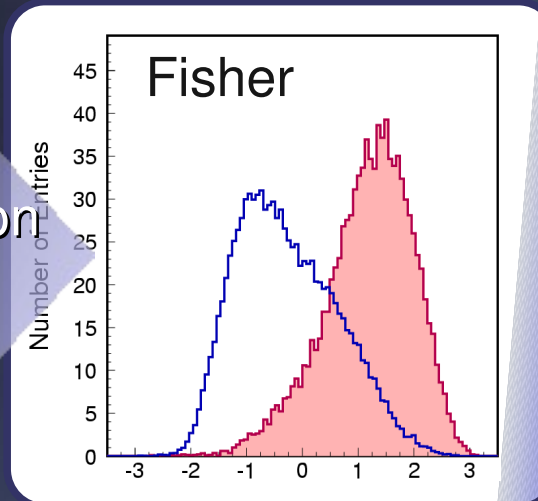
$e^+e^- \rightarrow q\bar{q}$



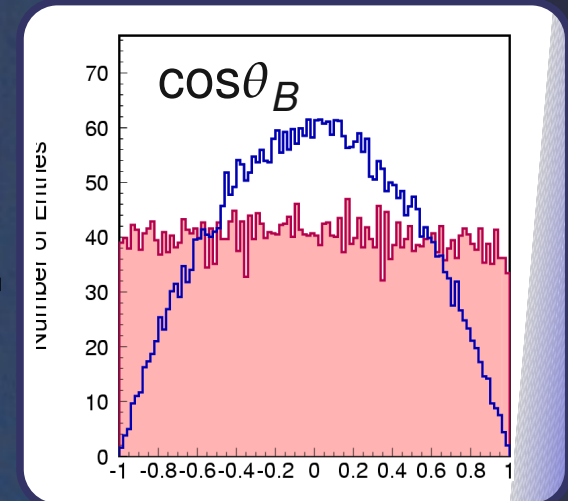
# Continuum Suppression



Project  
to 1-dimension  
by a Fisher  
Discriminat

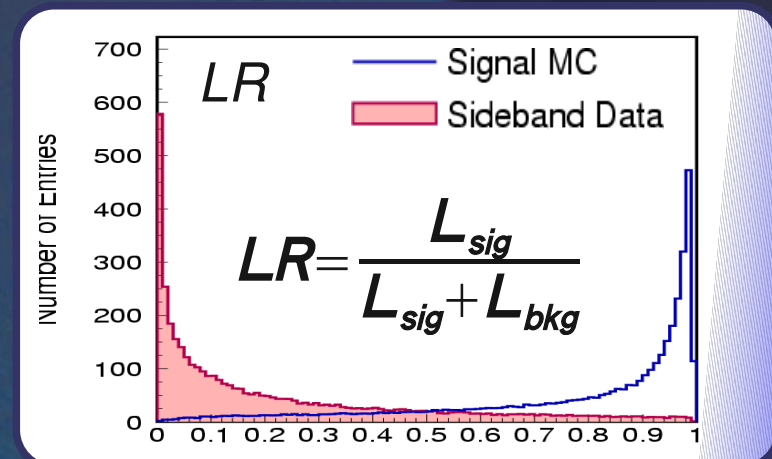


+

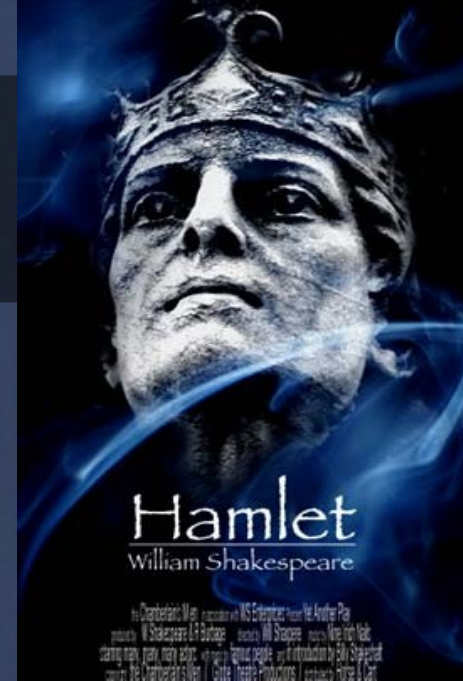
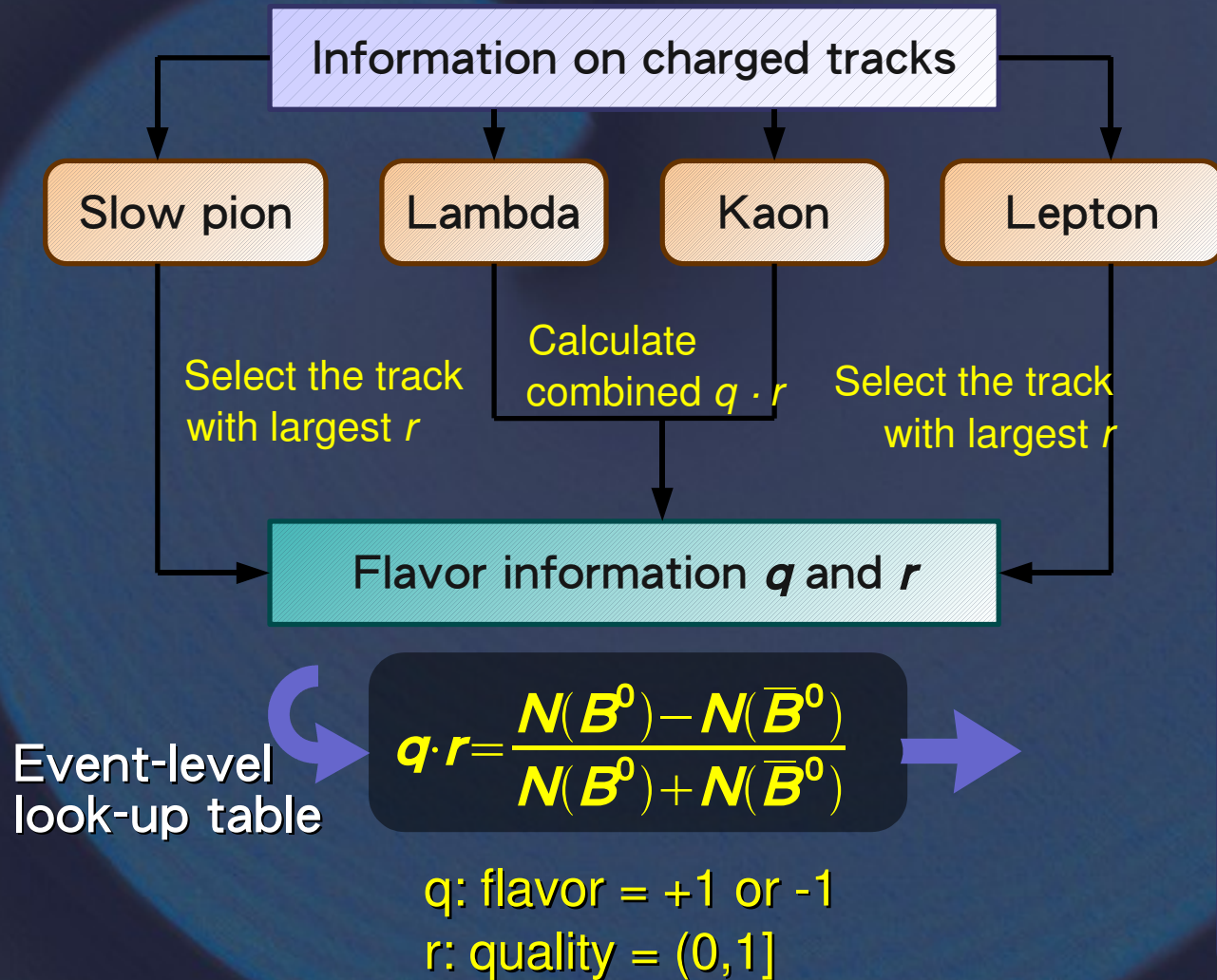


=

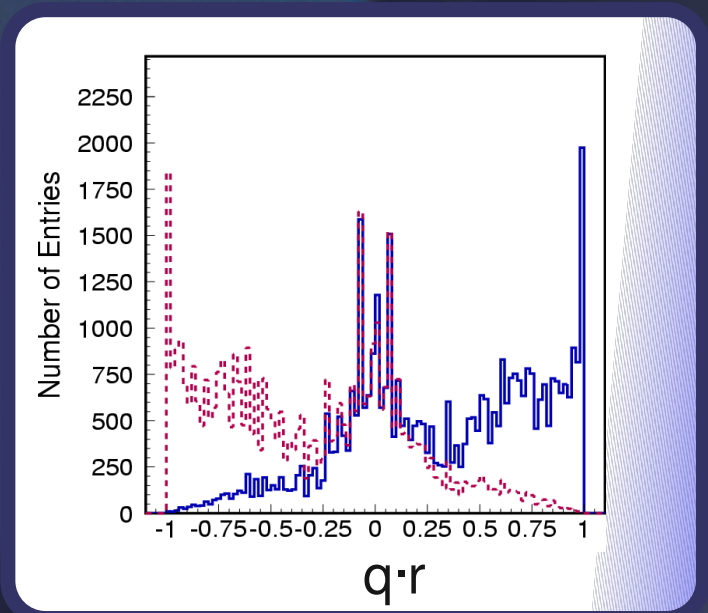
- ❑ Naïve error:  $\delta S_f \propto 1/\sqrt{N_S} \propto \sqrt{(1 + N_B/N_S)}$
- ❑ Most of the Belle analysis use a likelihood ratio to combine all the information, while many BaBar analysis use the neural network.
- ❑ Selection applied on the final LR/NN.



# Flavor Tagging



To **B** or not to **B**, that's a question





# Flavor Tagging

## Tagging Performance

- A replacement for real data:

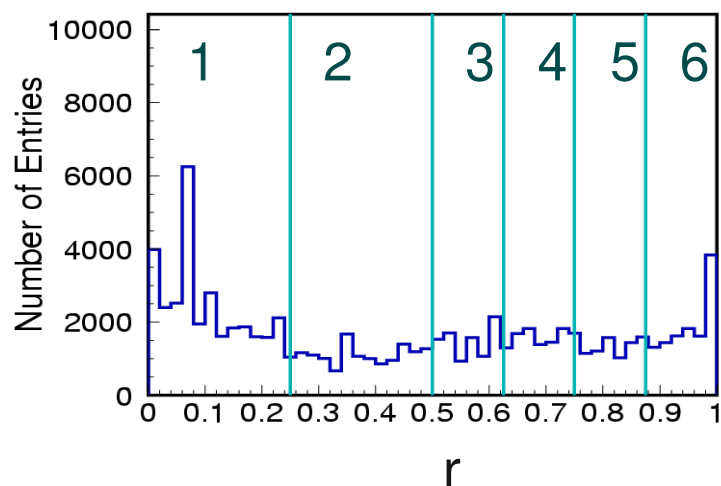
$$q \cdot r = q(1 - 2w_{tag})$$



wrong-tag fractions

- Wrong-tag fractions are measured by the *B*-mixing study in 6 'r' regions, and the performance is rated by the effective efficiency:

$$\epsilon_{eff} = \sum_l \epsilon (1 - 2w_{tag}^l) \approx \mathbf{29\%}$$



| DS-I | <i>r</i> interval | $w_l$             | $\Delta w_l$       | $\epsilon_{eff,l}$ |
|------|-------------------|-------------------|--------------------|--------------------|
| 1    | 0.000 – 0.250     | $0.464 \pm 0.006$ | $-0.011 \pm 0.006$ | $0.002 \pm 0.001$  |
| 2    | 0.250 – 0.500     | $0.331 \pm 0.008$ | $+0.004 \pm 0.010$ | $0.017 \pm 0.002$  |
| 3    | 0.500 – 0.625     | $0.231 \pm 0.009$ | $-0.011 \pm 0.010$ | $0.030 \pm 0.002$  |
| 4    | 0.625 – 0.750     | $0.163 \pm 0.008$ | $-0.007 \pm 0.009$ | $0.055 \pm 0.003$  |
| 5    | 0.750 – 0.875     | $0.109 \pm 0.007$ | $+0.016 \pm 0.009$ | $0.057 \pm 0.002$  |
| 6    | 0.875 – 1.000     | $0.020 \pm 0.005$ | $+0.003 \pm 0.006$ | $0.126 \pm 0.003$  |

# Understanding the $\Delta t$

- Resolution function: describe the smearing due to detector or physics.
- $\Delta t$  probability density function:

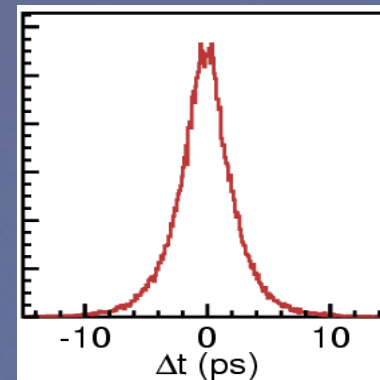
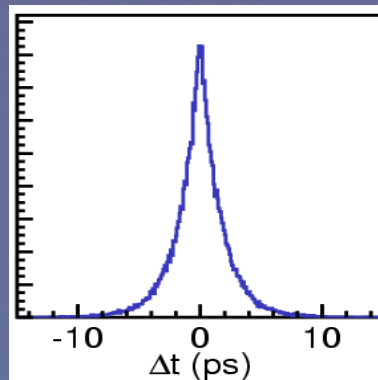
Convolution

$$P(\Delta t) = \int_{-\infty}^{+\infty} d(\Delta t') P(\Delta t') R(\Delta t - \Delta t')$$

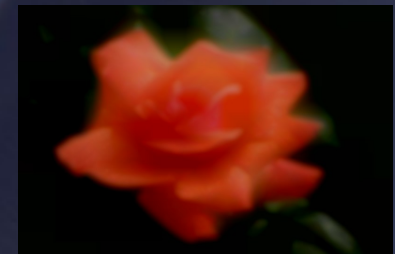
True  $\Delta t$  PDF  $\Leftarrow$  Gaussian-based resolution function.

- The resolution is consistent of three parts:  $R(\Delta t) = R_{det} \otimes R_{np} \otimes R_k$

True  $\Delta t$

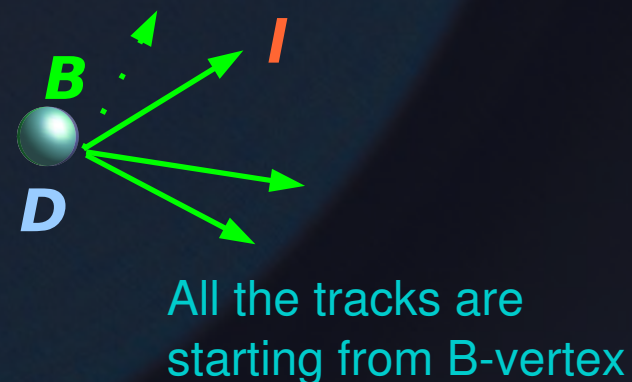
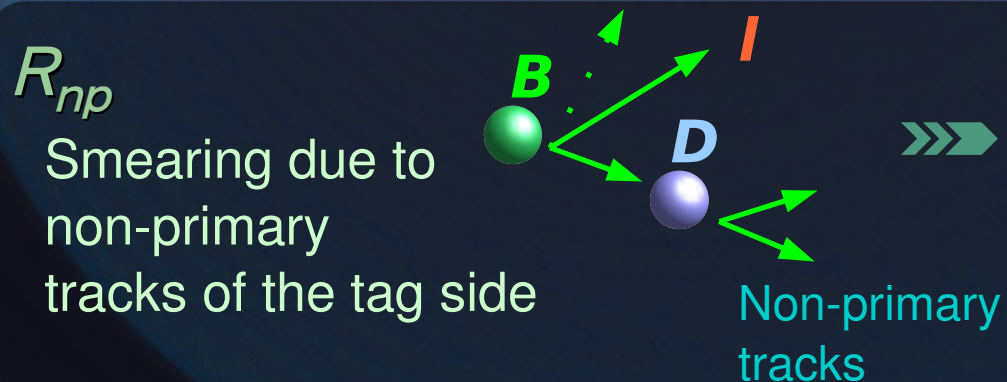
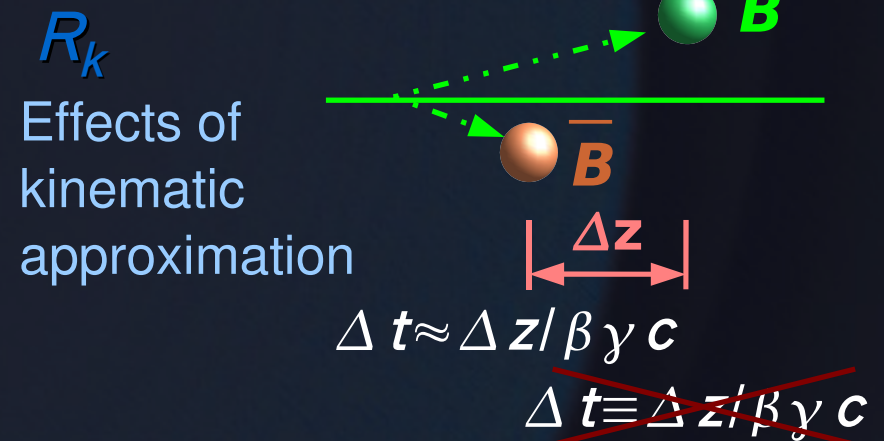
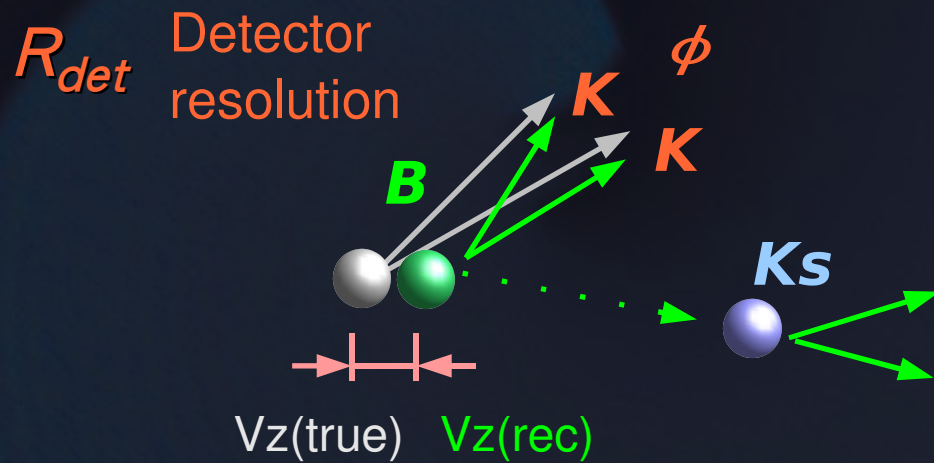


Measured  $\Delta t$



# Understanding the $\Delta t$

## Resolution Function





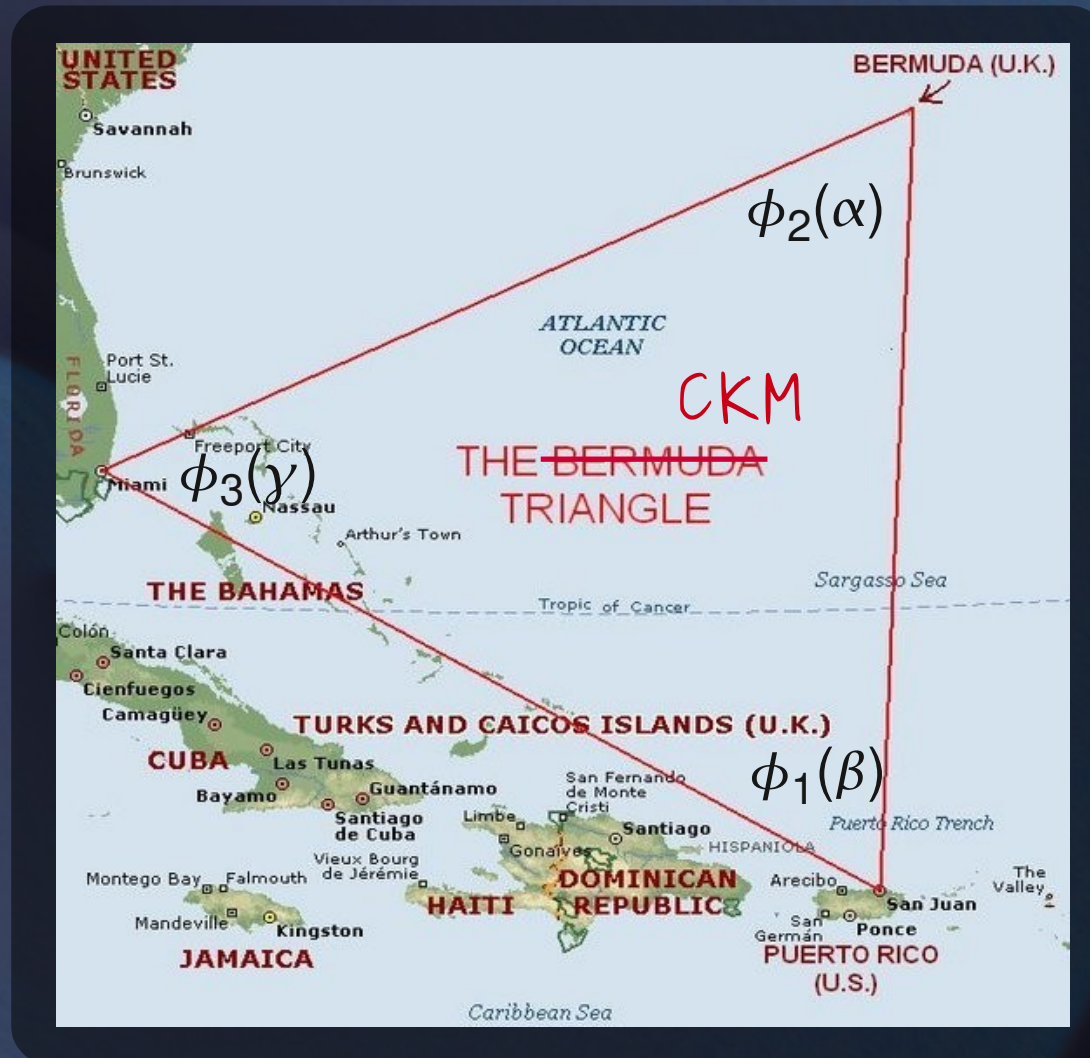
# Check List

# KEK / open box room

Before we see the data many items have been cross-checked

Before we see the data  
many items have been  
cross-checked

- 1) Lifetime of  $f_{CP}$
- 2) Lifetime of control sample
- 3)  $CP$ -fit with control sample
- 4)  $CP$ -fit with signal MC
- 5)  $CP$ -fit w/o flavor
- 6)  $CP$ -fit w/ Toy MC



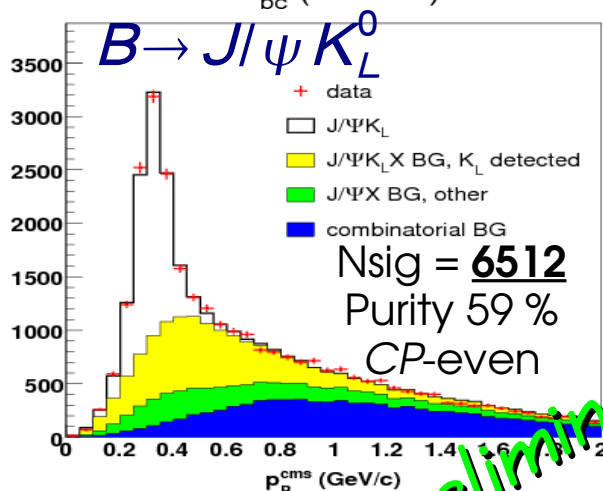
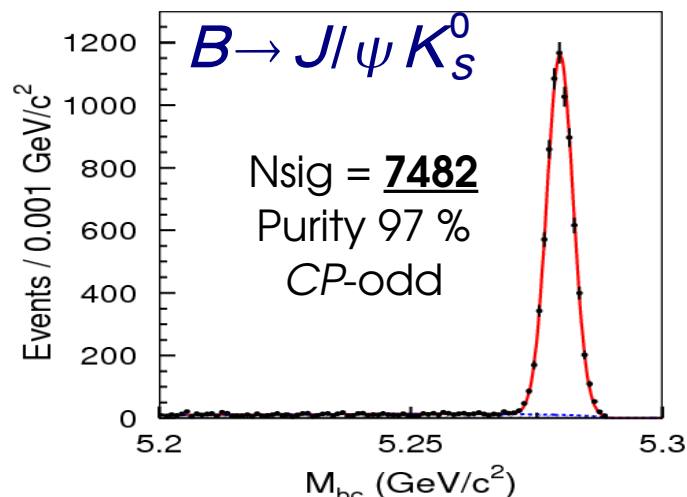
# Measurements of the CKM Triangle



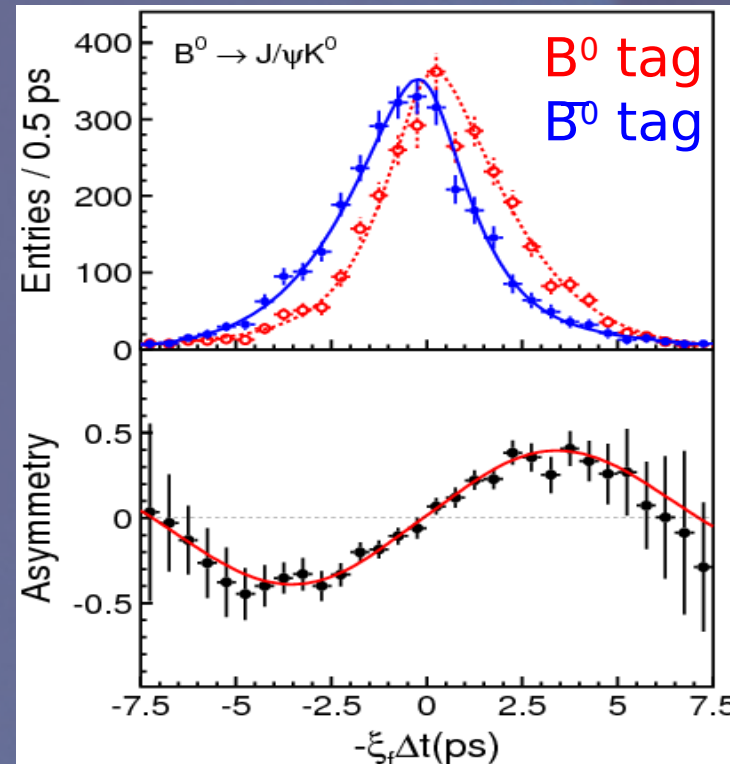
# Measurement of $\sin 2\phi_1$



535M  $BB$  pairs



preliminary



$$\sin 2\phi_1 = 0.642 \pm 0.031 (\text{stat}) \pm 0.017 (\text{syst})$$

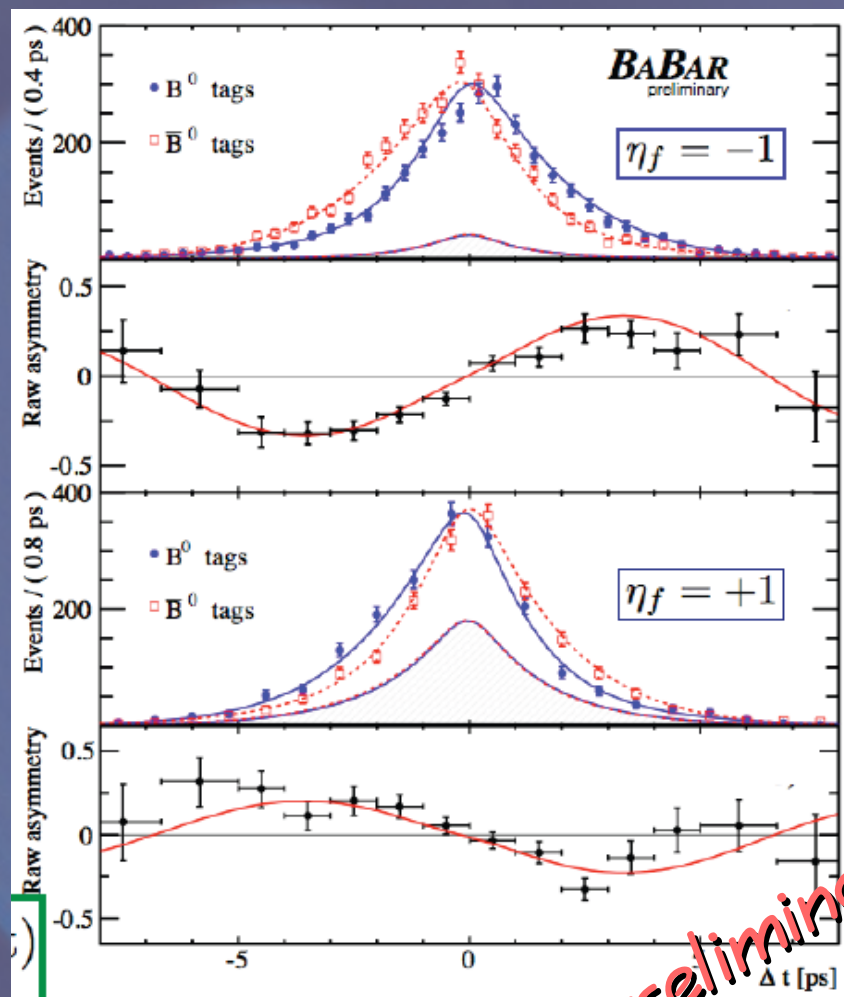
$$A = 0.018 \pm 0.021 (\text{stat}) \pm 0.014 (\text{syst})$$



# Measurement of $\sin 2\phi_1$



347M  $BB$  pairs



Included decays:

$$B \rightarrow J/\psi K^0$$

$$B \rightarrow \psi(2S) K_S$$

$$B \rightarrow \eta_c K_S$$

$$B \rightarrow \chi_{c1} K_S$$

$$B \rightarrow J/\psi K^{*0}$$

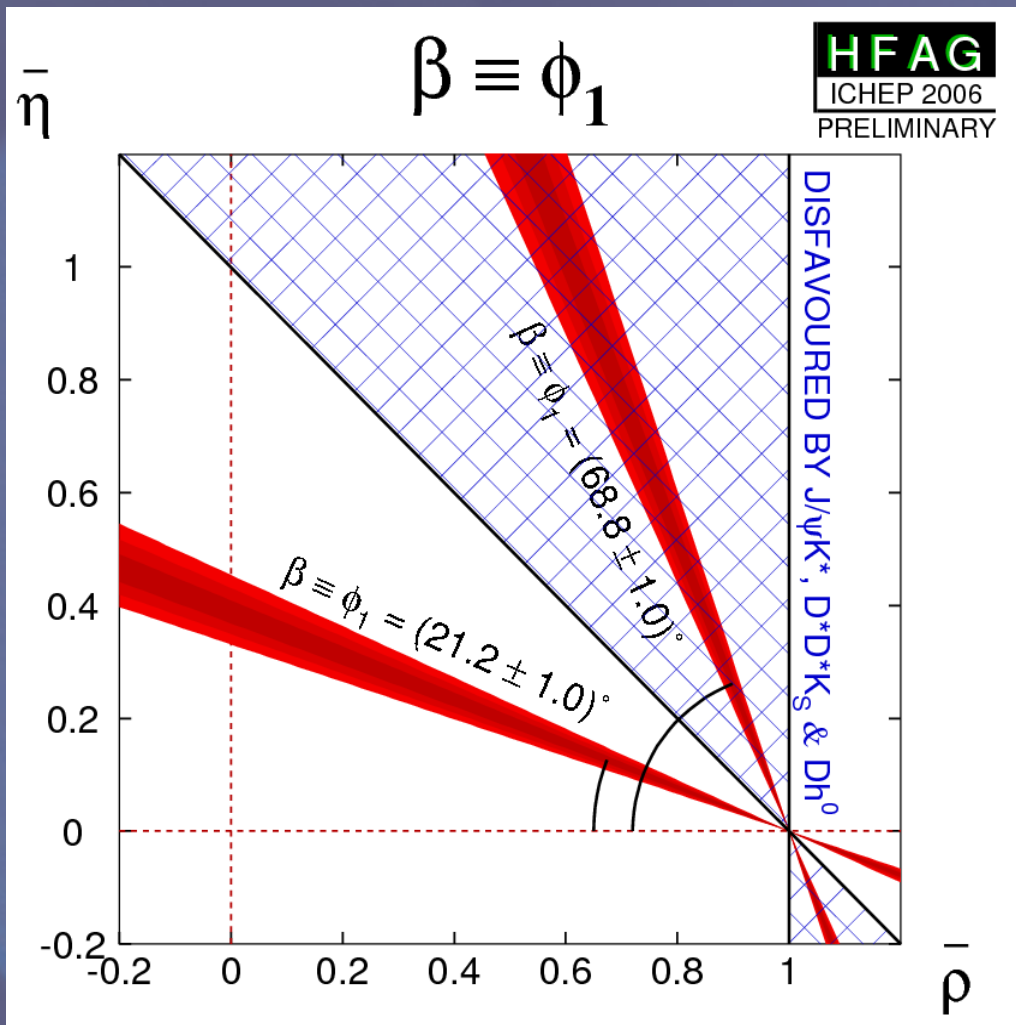
$$\sin 2\phi_1 = 0.710 \pm 0.034 \pm 0.019$$

$$|\lambda| = 0.932 \pm 0.026 \pm 0.017$$

$$(A = -0.07 \pm 0.026 \pm 0.018)$$

preliminary

# Measurement of " $\phi_1$ "



$$\langle \sin 2\phi_1 \rangle = 0.674 \pm 0.026$$



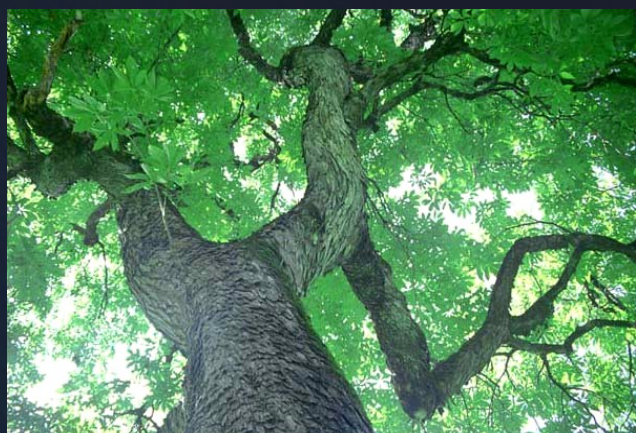
- Time-dependent Dalitz analysis on  $B^0 \rightarrow D^* D^* K_S$ :  $\cos 2\phi_1 > 0$  @ 94% C.L., (model-dependent)



- Time-dependent Dalitz analysis on  $B^0 \rightarrow D^0 h^0$ :  $\cos 2\phi_1 > 0$   
@ 98.3% C.L., (Belle)  
@ 87% C.L., (BaBar)

# TCPV in $b \rightarrow s$ Transitions

- ❑ The Standard Model explains almost all observed  $CP$  asymmetries to date.
- ❑ But it is known to be incomplete.
- ❑ A good place to search for physics beyond the SM is provided by measuring the  $CP$  violation in  $b \rightarrow sqq$  penguin processes, and compare it with the  $b \rightarrow ccs$  decays.



$b \rightarrow c$  Tree

New Physics  
in the loop  
diagram!?

$\neq ?$



$b \rightarrow s$  Penguins



# $b \rightarrow s$ Sensitive Decays

$$\phi K_S / \phi K_L$$

- ✓ Smallest theoretical error
- ✓ Clean ( $K_S$ )

$$\eta' K_S / \eta' K_L$$

- ✓ Largest BF
- ✓ Clean ( $\eta' \rightarrow \eta \pi \pi$ )

$$K_S K_S K_S$$

- ✗ Require special  $K_S$  vertex
- ✓ Clean, clear  $CP$  state

$$f_0 K_S$$

- ✗ Unclear  $f_0$  resonance

$$K^+ K^- K_S / K^+ K^- K_L$$

- ✓ Large BF
- ✗ Unclear  $CP$  state

$$\pi^0 K_S$$

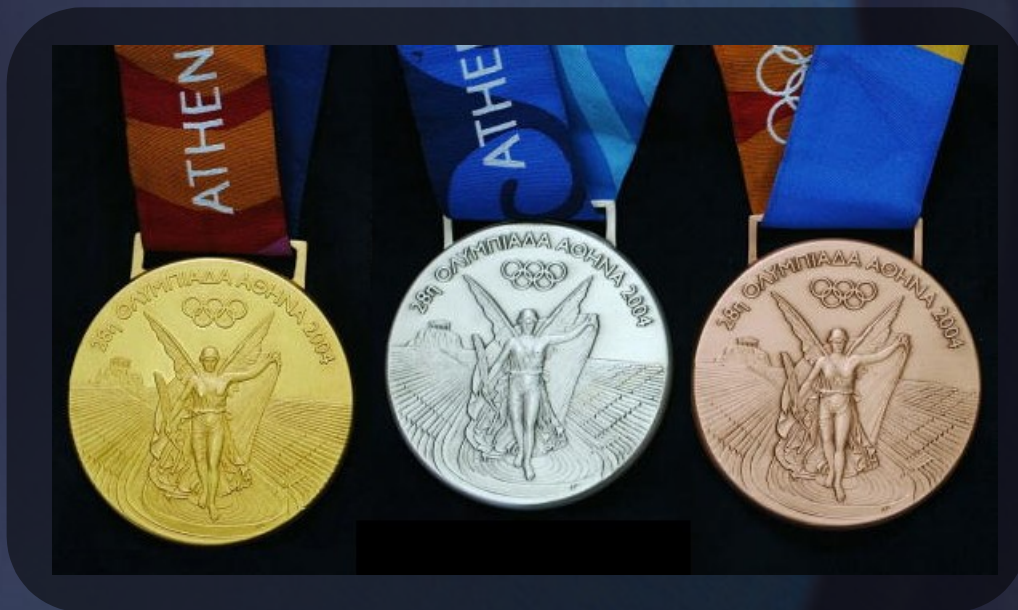
- ✗ Require special  $K_S$  vertex tech.
- ✓ Supports  $B \rightarrow K \pi$  DCPV ( $\pi^0 K_S$ )

$$\omega K_S$$

- ✗ Large theoretical error
- ✗ Dirty / Small signal

$$\pi^0 \pi^0 K_S$$

- ✗ Special  $K_S$  vertex tech.
- ✗ Very Dirty

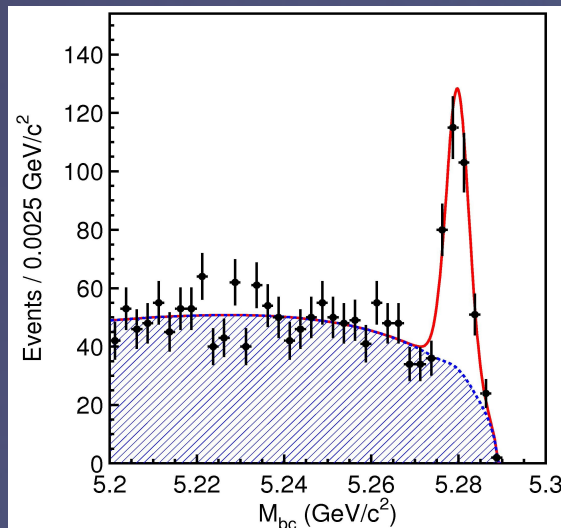
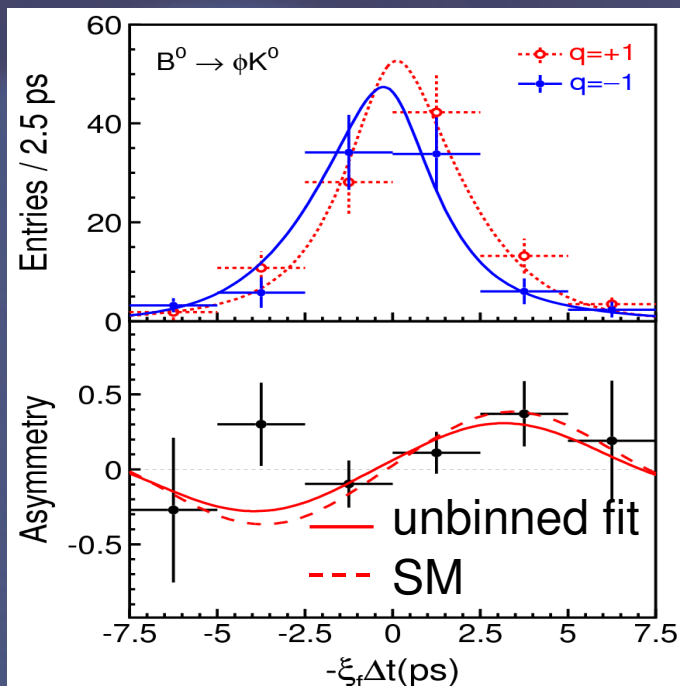


# TCPV in $B \rightarrow \phi K^0$

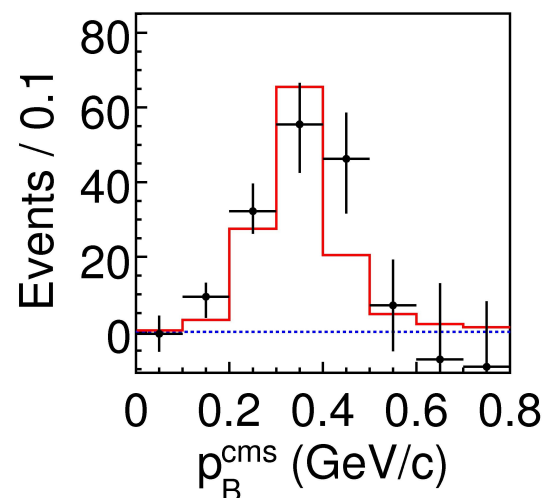


535M  $BB$  pairs

↙ Good Tags only & bkg. subtracted



$$N(\phi K_S) = 307 \pm 21$$



$$N(\phi K_L) = 114 \pm 17$$

$$“\sin 2\phi_1” = 0.50 \pm 0.21 \pm 0.06$$

$$A = 0.07 \pm 0.15 \pm 0.05$$

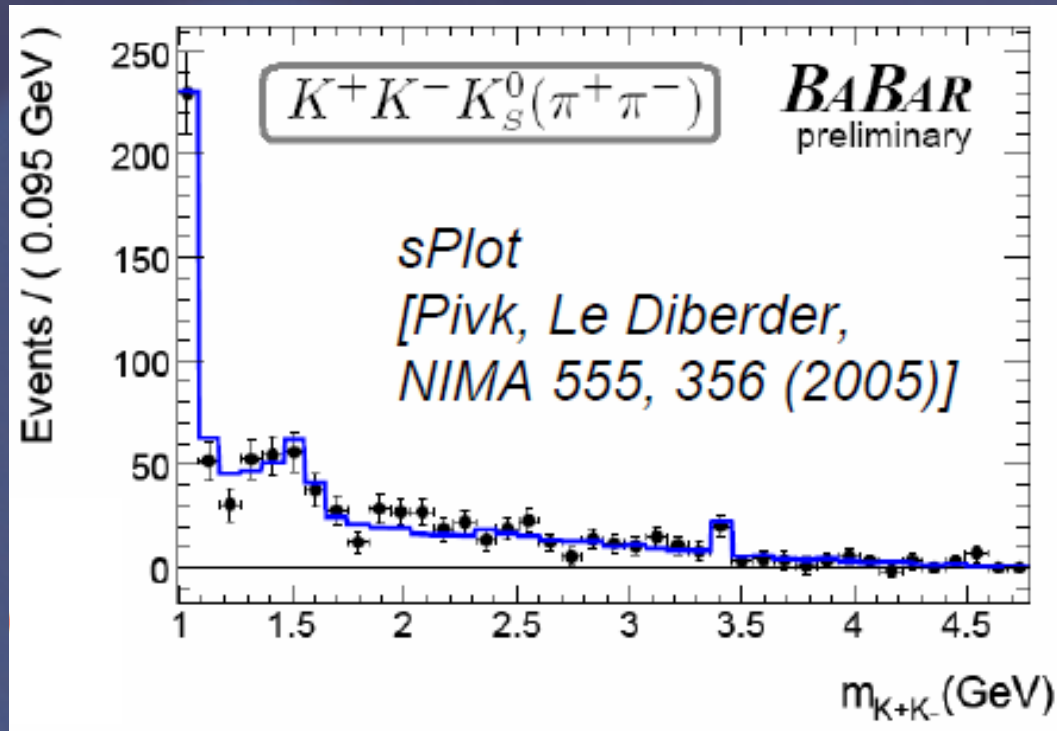
preliminary

- Consistent with SM prediction ( $\sim 1\sigma$ ).
- Consistent with Belle 2005 result ( $S = 0.44 \pm 0.27 \pm 0.05$ )

# TCPV in $B \rightarrow KKK^0$ Dalitz



347M  $BB$  pairs



*Model=*

$\phi(1020)K + f_0(980)K + NR +$   
 $X_0(1550)K + \chi_{c0}K + DK + D_S K$

$$N(K^+ K^- K^0) = 1516 \pm 65$$

$$\left\{ \begin{array}{l} B^0 \rightarrow K^+ K^- K_S^0(\pi^+ \pi^-) \\ B^0 \rightarrow K^+ K^- K_S^0(\pi^0 \pi^0) \\ B^0 \rightarrow K^+ K^- K_L^0 \end{array} \right.$$

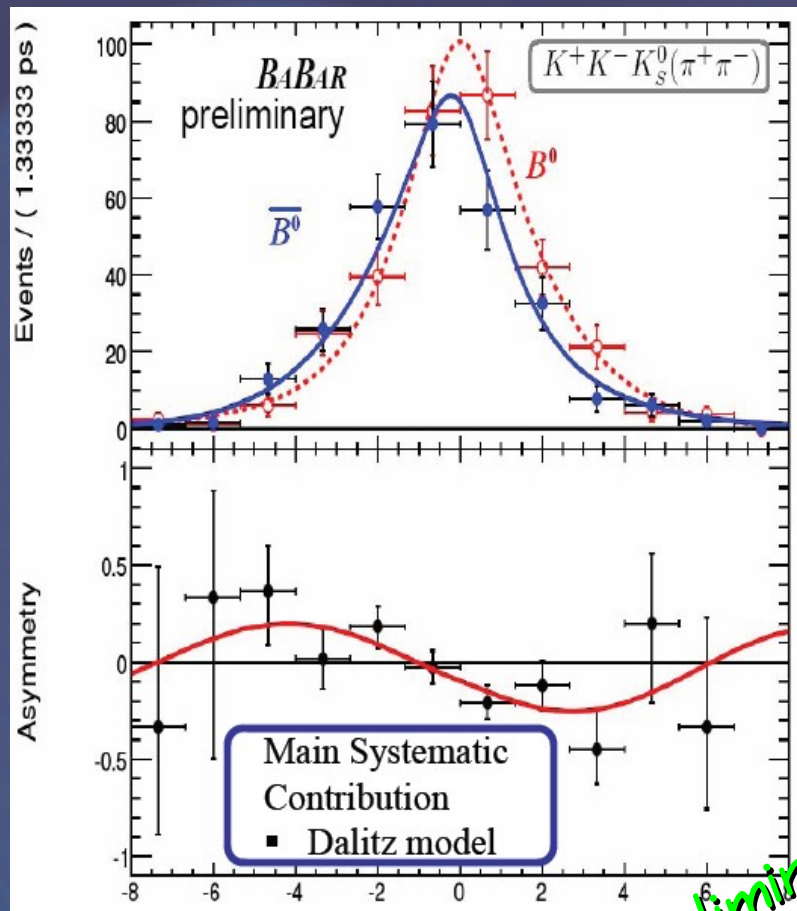
- ❑ Obtain  $CP$  parameters for 2-body and 3-body modes simultaneously by time-dependent Dalitz fits.
- ❑ Fit to the low mass region in order to obtain the CPV parameters for  $\phi K_S$  and  $f_0(980)K_S$ .



# TCPV in $B \rightarrow KKK^0$ Dalitz



347M  $BB$  pairs



- Measurement on  $\phi_1$  (not  $\sin 2\phi_1$ ) w/ full region:

$$A_{CP} = -0.034 \pm 0.079 \pm 0.025$$
$$\phi_1^{\text{eff}} = 0.361 \pm 0.079 \pm 0.037$$

- Fits to low mass region:

$$A_{CP}(\phi K^0) = -0.18 \pm 0.20 \pm 0.10$$

$$\phi_1^{\text{eff}}(\phi K^0) = 0.06 \pm 0.16 \pm 0.05$$

$$A_{CP}(f_0 K^0) = 0.45 \pm 0.28 \pm 0.10$$

$$\phi_1^{\text{eff}}(f_0 K^0) = 0.18 \pm 0.19 \pm 0.04$$

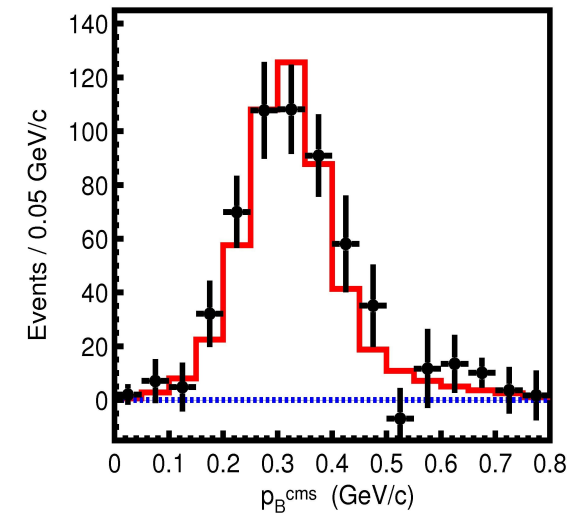
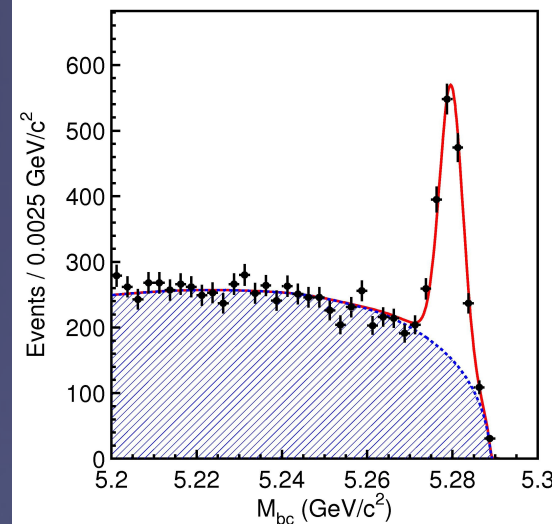
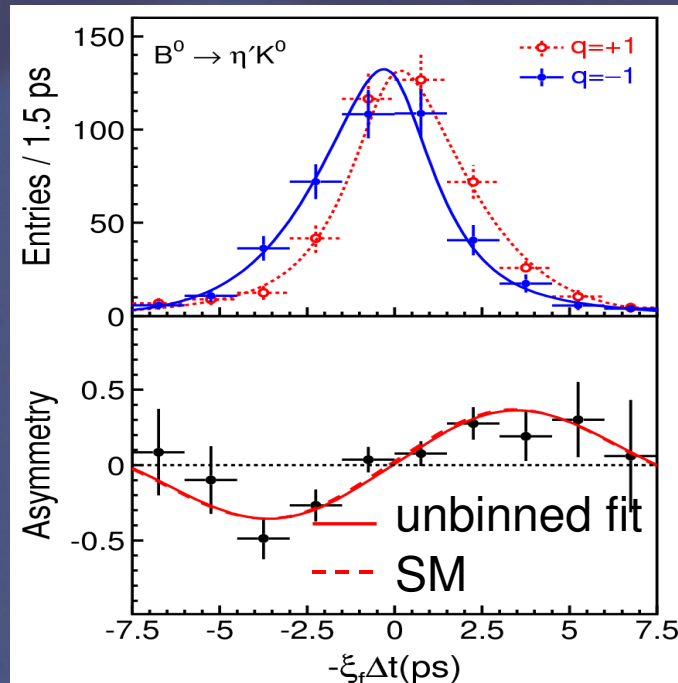
$$\sin 2\phi_1(\phi K^0) = +0.12 \pm 31 \pm 0.10$$

# TCPV in $B \rightarrow \eta' K^0$



535M  $BB$  pairs

↙ Good Tags only & bkg. subtracted



$$N(\eta' K_S) = 1421 \pm 46 \quad N(\eta' K_L) = 454 \pm 39$$

$$\text{"sin} 2\phi_1\text{"} = 0.64 \pm 0.10 \pm 0.04$$

$$A = -0.01 \pm 0.07 \pm 0.05$$

preliminary

- First observation of TCPV ( $5.6\sigma$ ) in a single  $b \rightarrow s$  decay mode.
- Consistent with SM prediction.

# TCPV in $B \rightarrow \eta' K^0$

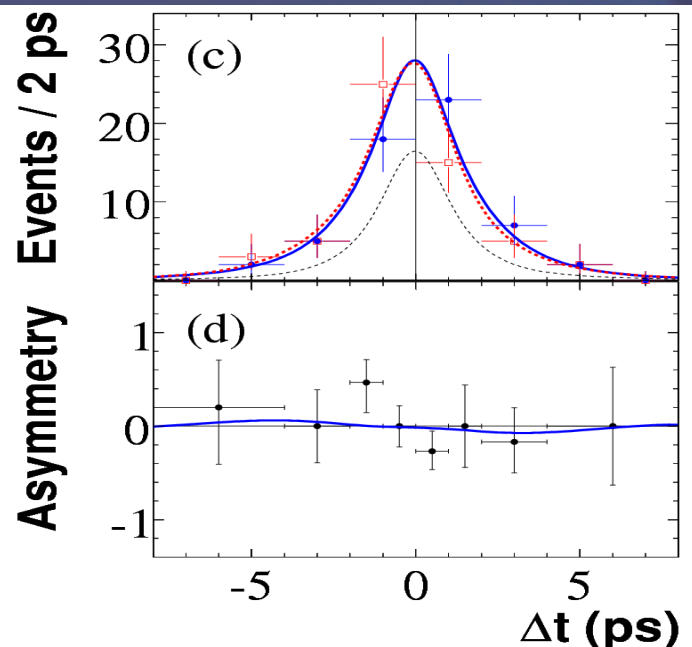
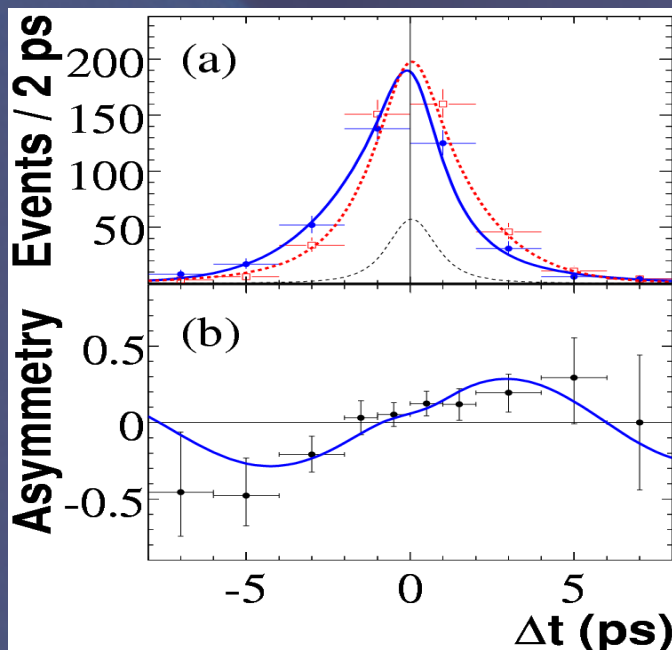


384M  $BB$  pairs

$$N(\eta' K_S) = 1038 \pm 44$$

$$N(\eta' K_L) = 204 \pm 24$$

$\eta' K_S$



$\eta' K_L$

$$“\sin 2\phi_{\eta'}” = 0.58 \pm 0.10 \pm 0.03$$

$$A = 0.16 \pm 0.07 \pm 0.03$$

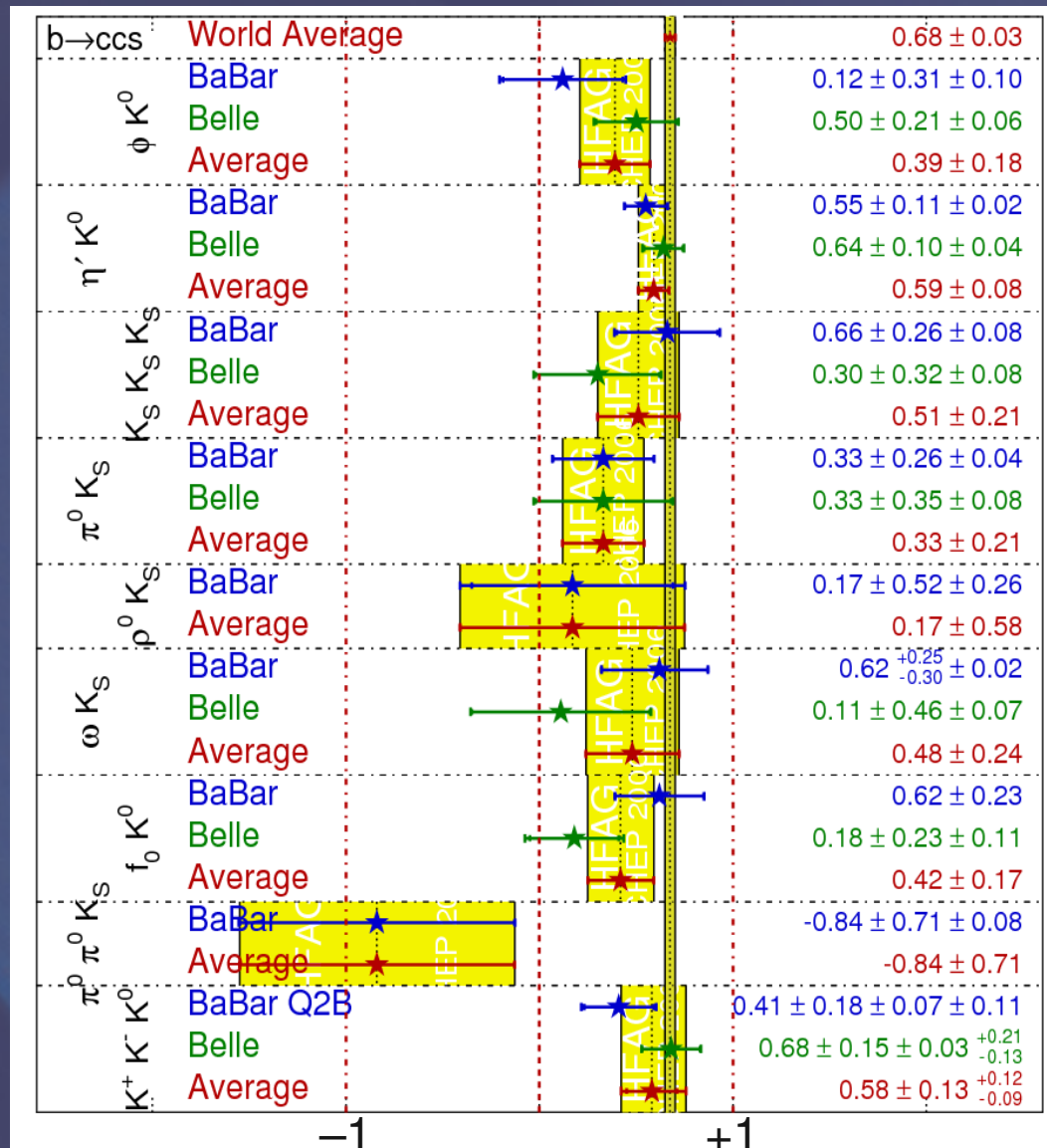
5.5 $\sigma$  away from zero.

Consistent with SM prediction.

preliminary  
(2006 September)



# Other Penguin Modes



← HFAAG summer 2006 results

All measured values are smaller than the  $\sin 2\phi_1$  from  $b \rightarrow cc s$  decays.

Naïve average:  
 $S(\text{penguins}) = 0.52 \pm 0.05$   
 ( $\sim 2.6\sigma$  from  $S(b \rightarrow cc s)$ )

- The same analysis has been applied to 9 decay modes.
- More statistics are required for mode-by-mode studies.

# Signature on $\delta S_f$

- ❑ Even in the Standard Model, the expectations on  $S_f$  are not exactly equal to  $\sin 2\phi_1$ . e.g. the  $b \rightarrow u$  penguin is neglected, etc.
- ❑ Most of the measurements on  $\delta S$  are negative and small.  
How about the theory?
  - $\delta S$  bound from SU(3) relations
    - use the SU(3) relations to estimate the amplitudes  $\propto V_{ub}^* V_{us}$
    - providing boundaries on  $\delta S_f$  and  $A_f$ .
  - Factorization approaches:
    - annihilation, vertex corrections, final state interactions, etc.
    - providing model-dependent estimations on  $\delta S_f$ .

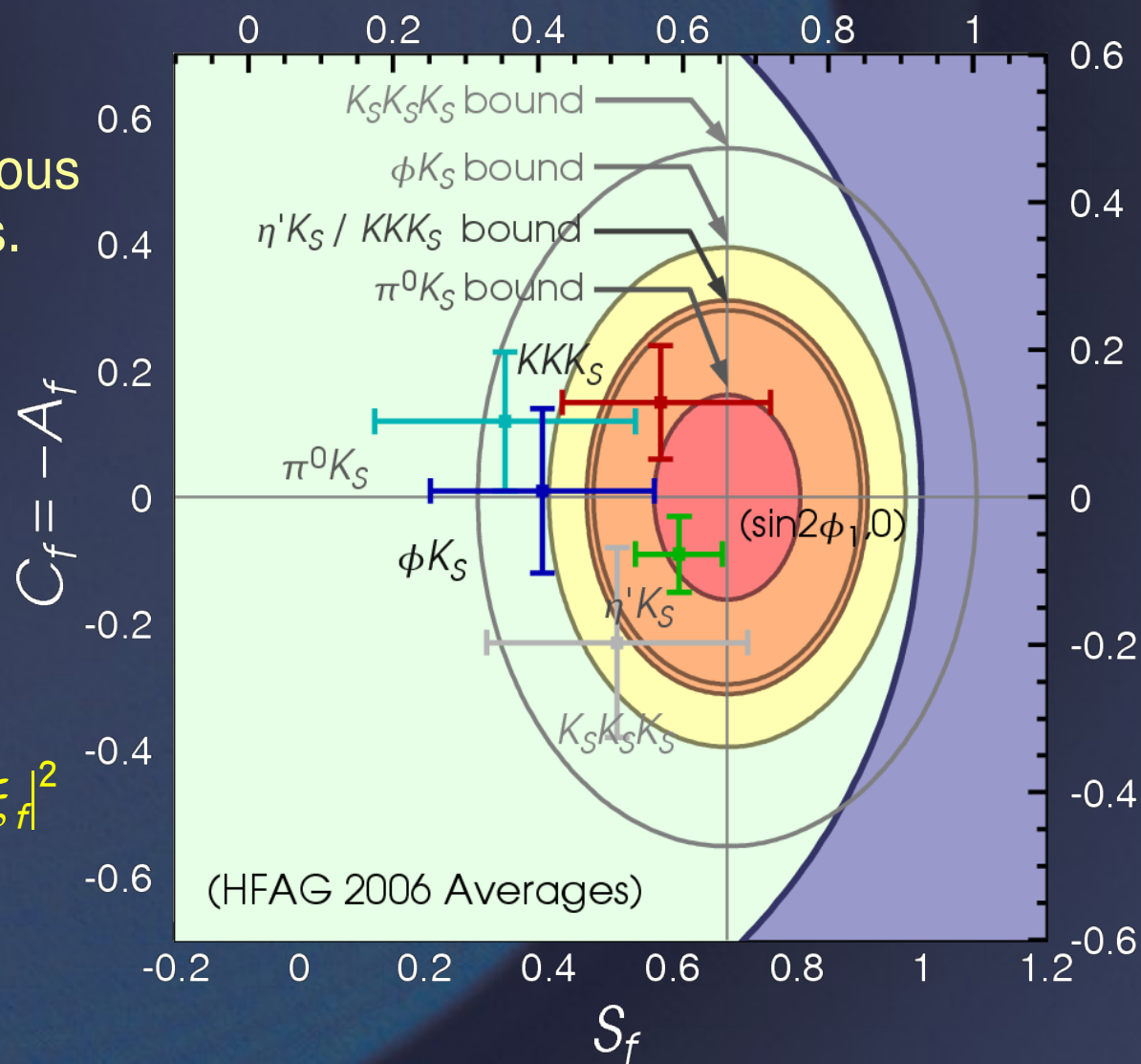
# $\delta S_f$ Bounds from SU(3) Relations

- SU(3) relations based on various charmless branching fractions. (from HFAG 2006 summer).

[Grossman, PRD68 (2003), 015004]  
 [Gronau, PLB579 (2004), 331-339]  
 [Engelhard, PRD72 (2005) 075013]

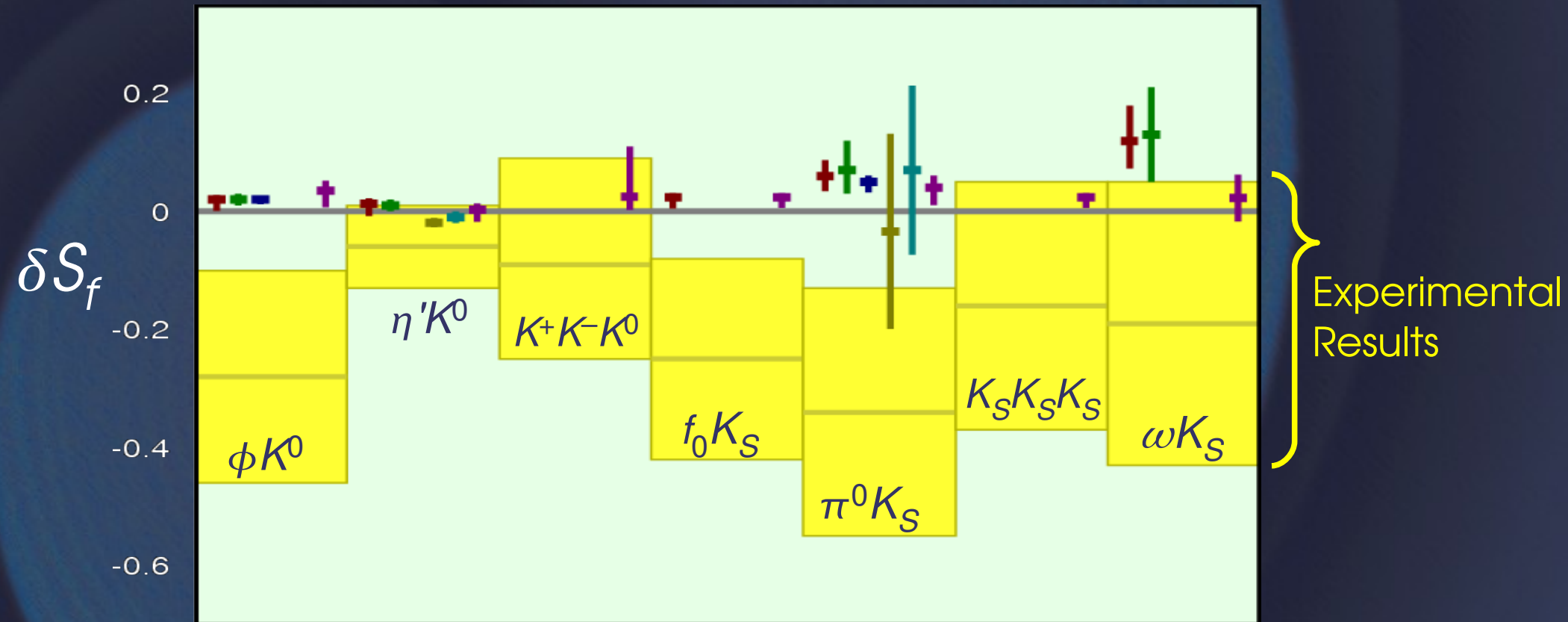
$$C_f^2 + \left[ \frac{\eta_f S_f + \sin 2\phi_1}{\cos 2\phi_1} \right]^2 = 4 \sin^2 \phi_3 |\xi_f|^2$$

$(\phi_3 \approx 63^\circ, \sin 2\phi_1 = 0.674)$



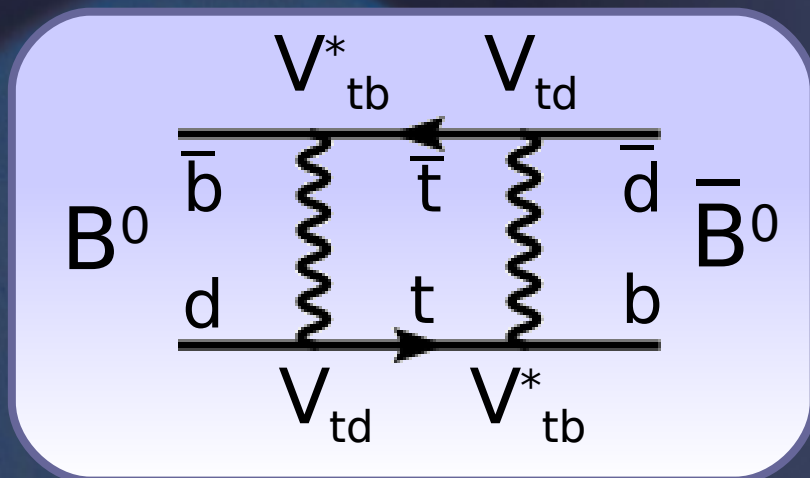


# Factorization Approaches

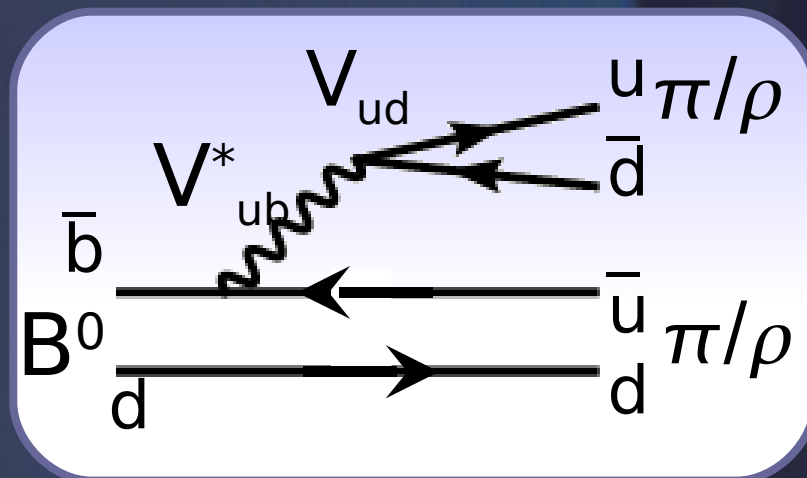


- QCDF (Cheng-CKC-Soni),    ■ QCDF+FSI (Cheng-CKC-Soni)
- QCDF (Beneke),            ■ pQCD (Mishima-Li)
- SCET (Williamson-Zupan) Solution 1 / ■ Solution 2

# Measurement of $\phi_2$



Mixing diagram



Decay diagram (tree)

Probing CKM angle  $\phi_2$   
in three directions:

$$\left\{ \begin{array}{l} B \rightarrow \pi^+ \pi^-, \pi^\pm \pi^0, \pi^0 \pi^0 \text{ +TCPV \& BR} \\ B \rightarrow \rho^+ \rho^-, \rho^\pm \rho^0, \rho^0 \rho^0 \text{ +TCPV + Angular Ana.} \\ B \rightarrow \rho^+ \pi^-, \rho^0 \pi^0 \text{ +TCPV + Dalitz} \end{array} \right.$$

# TCPV in $B \rightarrow \pi^+ \pi^-$

Time-dependent CP asymmetry in  $B \rightarrow \pi^+ \pi^-$  :

$$\mathbf{A}_{CP}(\mathbf{t}) = \mathbf{A}_{\pi\pi} \cos(\Delta m \mathbf{t}) + \mathbf{S}_{\pi\pi} \sin(\Delta m \mathbf{t})$$

$$\begin{aligned} \lambda &= e^{2i\phi_2} \\ \mathbf{A}_{\pi\pi} &= 0 \\ \mathbf{S}_{\pi\pi} &= \sin 2\phi_2 \end{aligned}$$

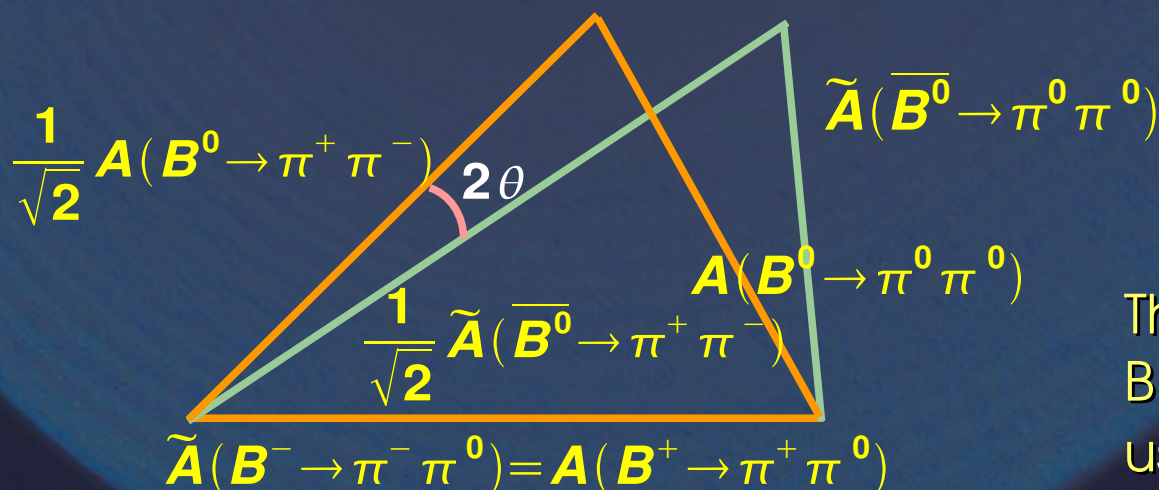
Tree only



$$\begin{aligned} \lambda &= e^{2i\phi_2} \frac{1 + |P/T| e^{i\delta} e^{i\gamma}}{1 + |P/T| e^{i\delta} e^{-i\gamma}} \\ \mathbf{A}_{\pi\pi} &\propto \sin \delta \\ \mathbf{S}_{\pi\pi} &= \sqrt{1 - \mathbf{A}_{\pi\pi}^2} \sin 2\phi_2^{\text{eff}} \end{aligned}$$

Tree + Penguin

Related to  $\phi_2$   
(isospin analysis required)



$$\theta = |\phi_2 - \phi_2^{\text{eff}}|$$

The branching fractions of  $B \rightarrow \pi^+ \pi^- / \pi^+ \pi^0 / \pi^0 \pi^0$  can be used to constrain  $\phi_2$

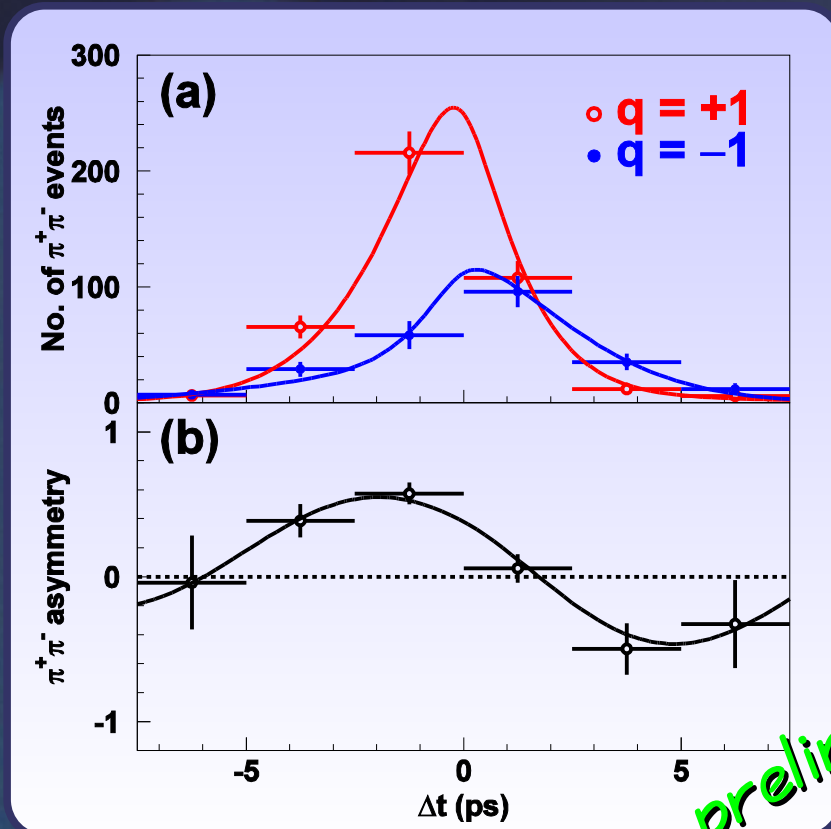


# TCPV in $B \rightarrow \pi^+ \pi^-$



535M  $BB$  pairs

↗ background subtracted



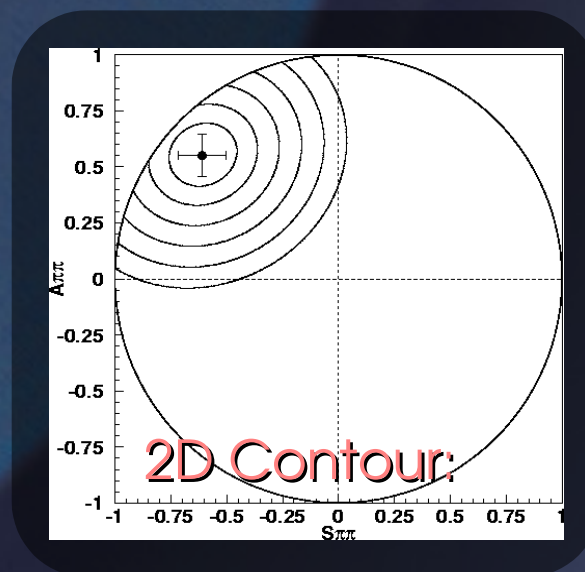
$$N(B \rightarrow \pi^+ \pi^-) = 1464 \pm 65$$

- Large direct  $CP$  violation ( $5.5\sigma$ ).
- Large mixing-induced  $CP$  violation ( $5.6\sigma$ ).

preliminary

$$A_{\pi\pi} = 0.55 \pm 0.08(\text{stat}) \pm 0.05(\text{syst.})$$

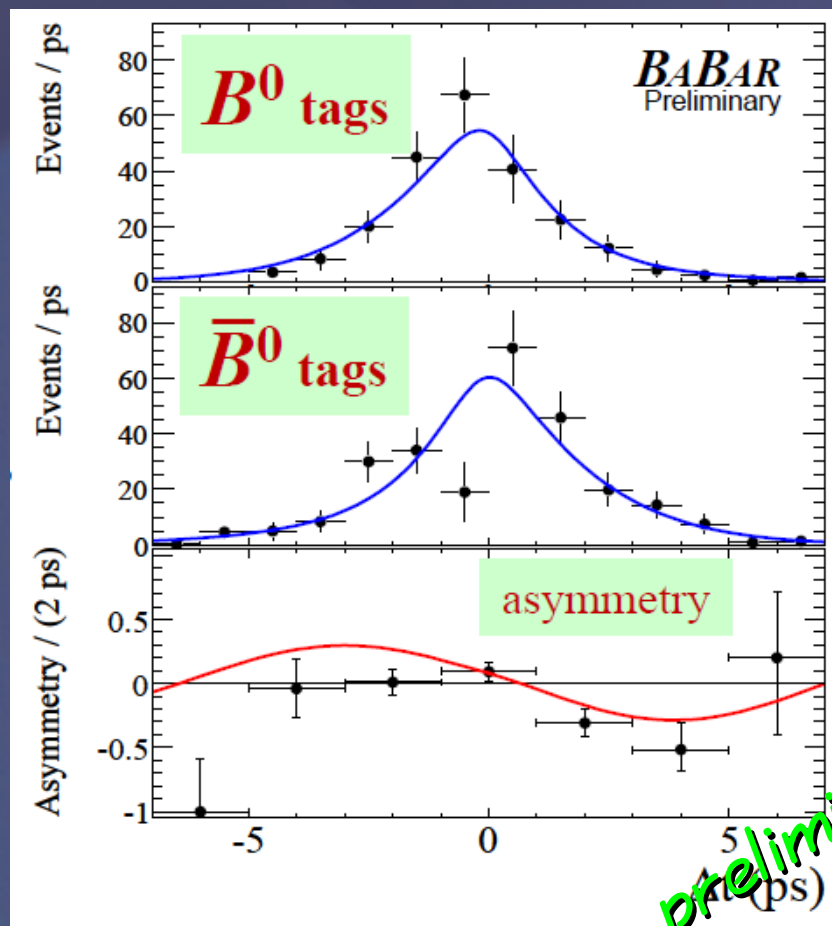
$$S_{\pi\pi} = -0.61 \pm 0.10(\text{stat}) \pm 0.04(\text{syst.})$$



# TCPV in $B \rightarrow \pi^+ \pi^-$



347M  $BB$  pairs

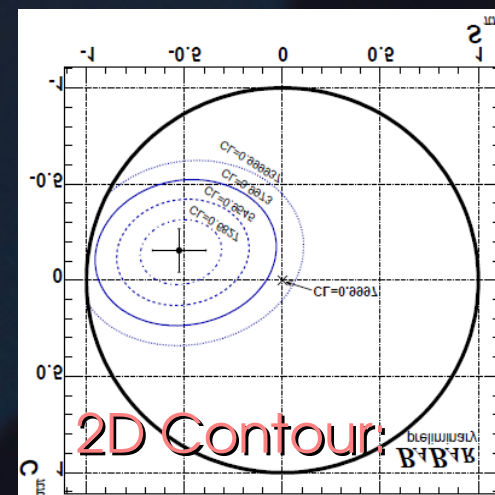


$$N(B \rightarrow \pi^+ \pi^-) = 675 \pm 42$$

- ☐ Evidence for  $CP$  violation ( $3.6\sigma$ ).
- ☐ No direct  $CP$  violation.

$$A_{\pi\pi} = 0.16 \pm 0.11(\text{stat}) \pm 0.03(\text{syst.})$$

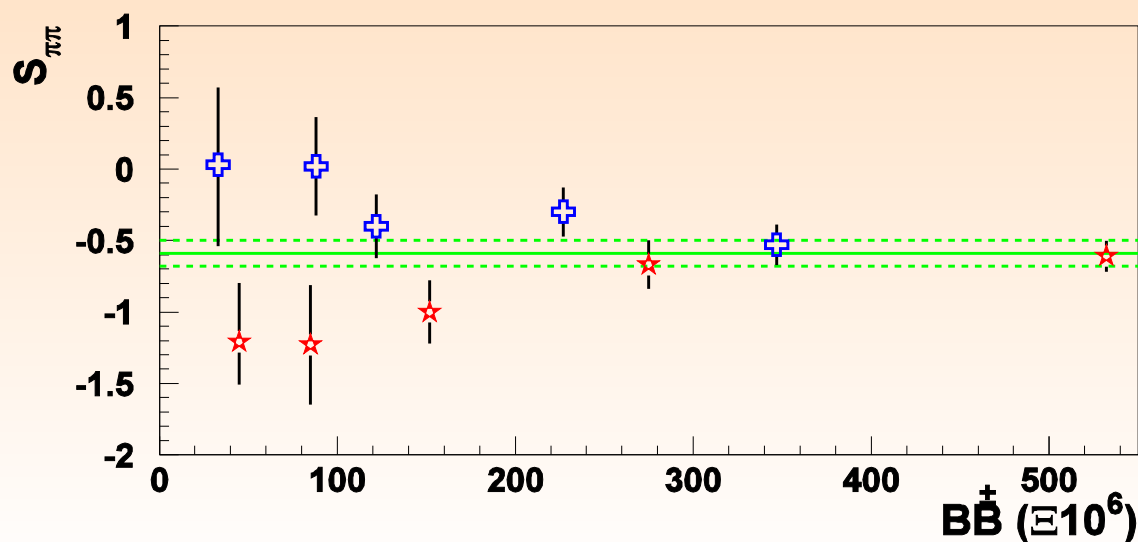
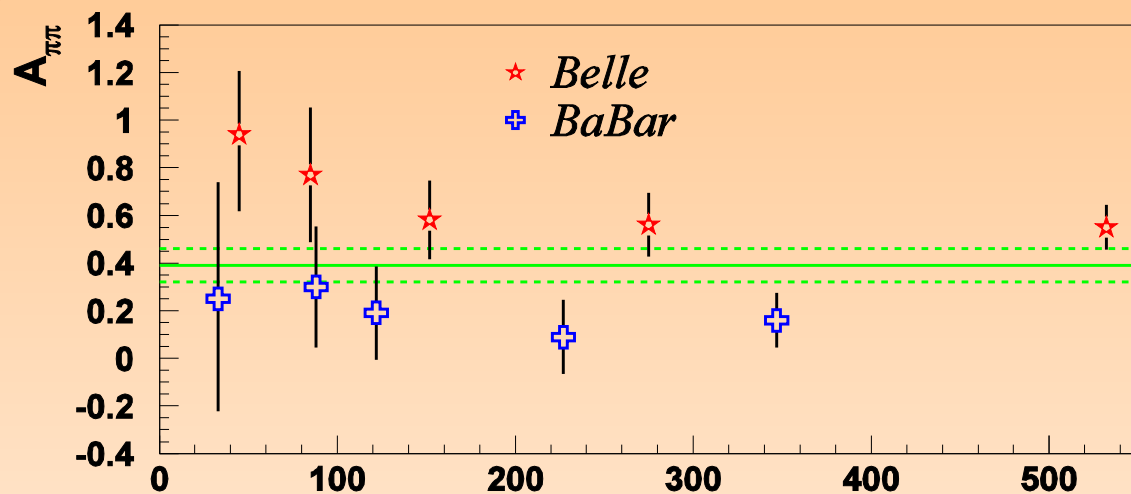
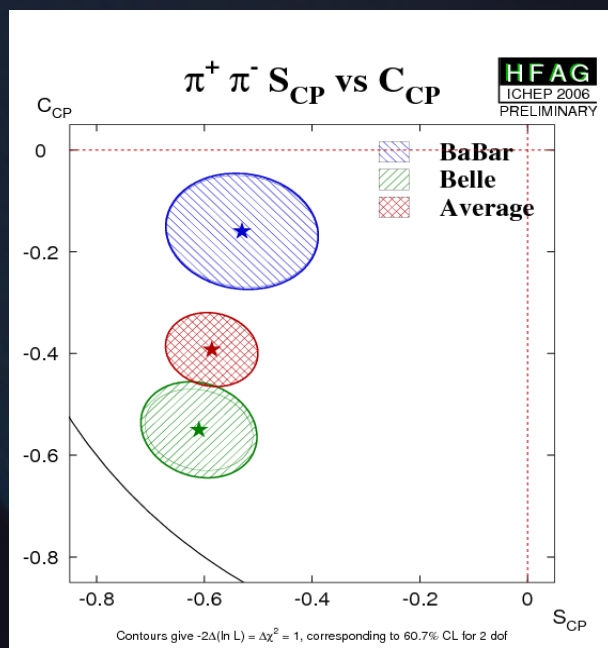
$$S_{\pi\pi} = -0.53 \pm 0.14(\text{stat}) \pm 0.02(\text{syst.})$$



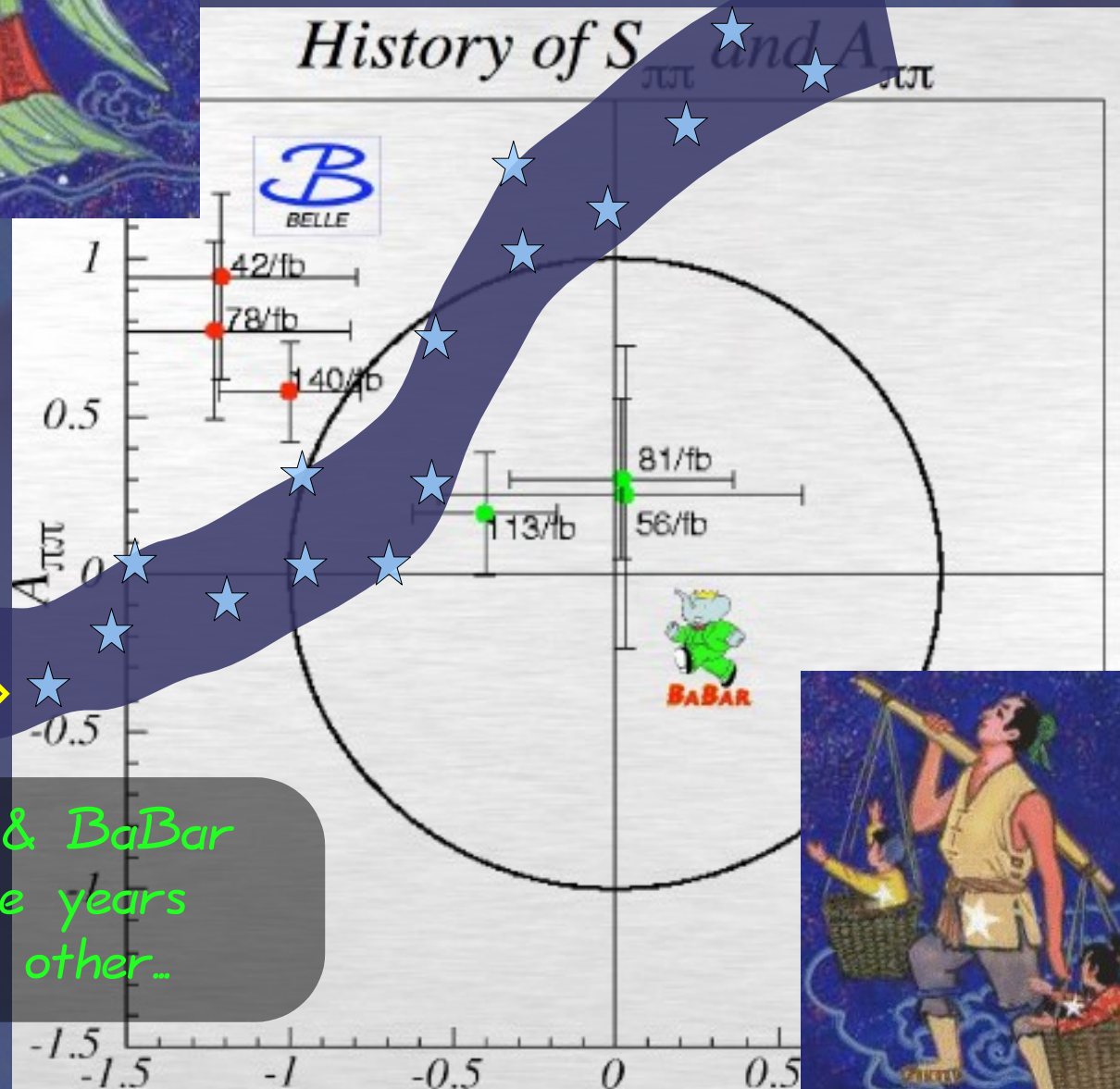
# TCPV in $B \rightarrow \pi^+ \pi^-$

□ Brief history of Belle & Babar measurements:

2.3 $\sigma$  difference  
between Belle & BaBar

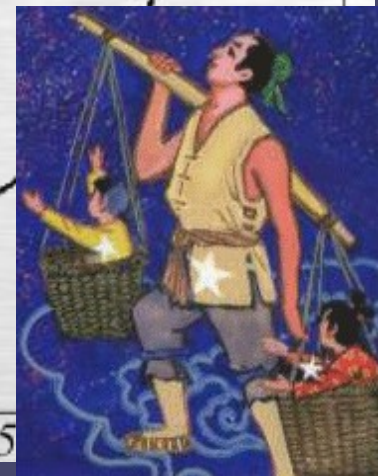




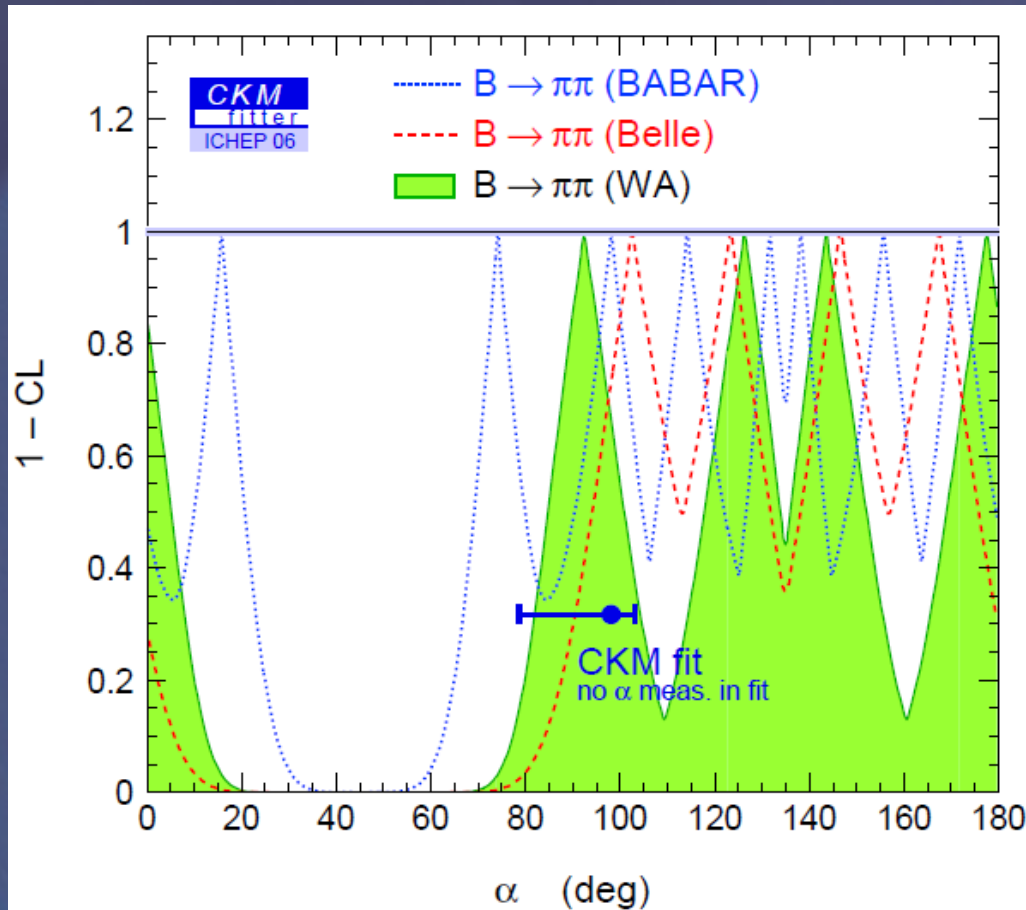


The Milky Way ➡

Probably, Belle & BaBar  
need few more years  
to meet each other..



# Measurement of $\phi_2$



## Inputs:

$$BR(B \rightarrow \pi^+ \pi^0) = 5.75 \pm 0.42 \times 10^{-6}$$

$$BR(B \rightarrow \pi^+ \pi^-) = 5.20 \pm 0.25 \times 10^{-6}$$

$$BR(B \rightarrow \pi^0 \pi^0) = 1.30 \pm 0.21 \times 10^{-6}$$

$$A_{CP}(B \rightarrow \pi^0 \pi^0) = +0.35 \pm 0.33$$

$$S(B \rightarrow \pi^+ \pi^-) = -0.59 \pm 0.09$$

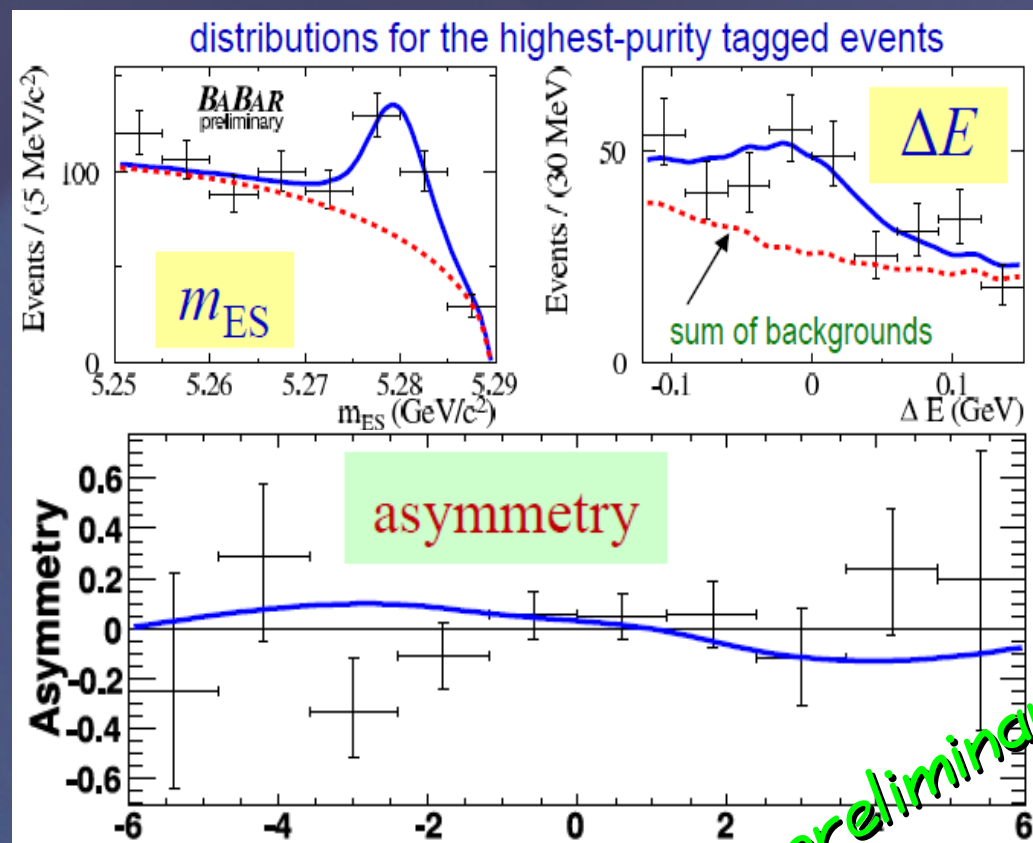
$$A(B \rightarrow \pi^+ \pi^-) = +0.39 \pm 0.07$$

- No stringent constraint obtained (many solutions!)
  - require  $\rho\pi/\rho\rho$  systems to solve it.

# TCPV in $B \rightarrow \rho^+ \rho^-$



347M  $BB$  pairs



$$N(B \rightarrow \rho^+ \rho^-) = 615 \pm 57$$

- $BR(\rho^+ \rho^-) > BR(\pi^+ \pi^-)$ .
- $BR(\rho^0 \rho^0) < BR(\pi^0 \pi^0)$   
(i.e. smaller penguin!)
- $f_L = 0.977 \pm 0.024$   
(i.e.  $\sim$  pure  $CP$ -even state,  
no needs of time-  
dependent angular analysis!)



275M Result:

$$S_{Long} = -0.19 \pm 0.21(\text{stat}) {}^{+0.05}_{-0.07}(\text{syst.})$$

$$C_{Long} = -0.07 \pm 0.15(\text{stat}) \pm 0.06(\text{syst.})$$

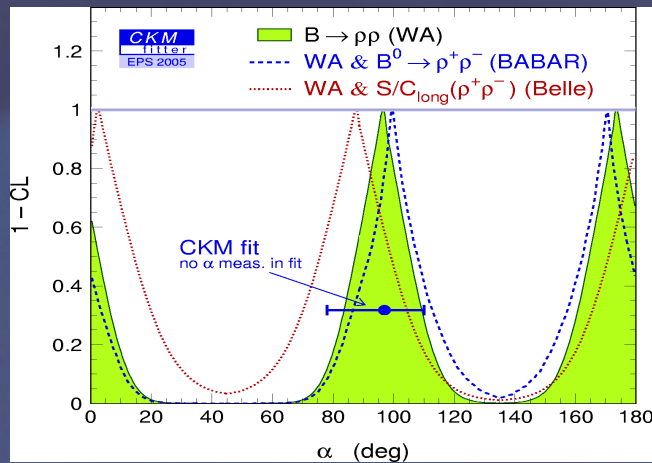
$$S_{Long} = 0.08 \pm 0.41 \pm 0.09$$

$$C_{Long} = 0.00 \pm 0.30 \pm 0.09$$



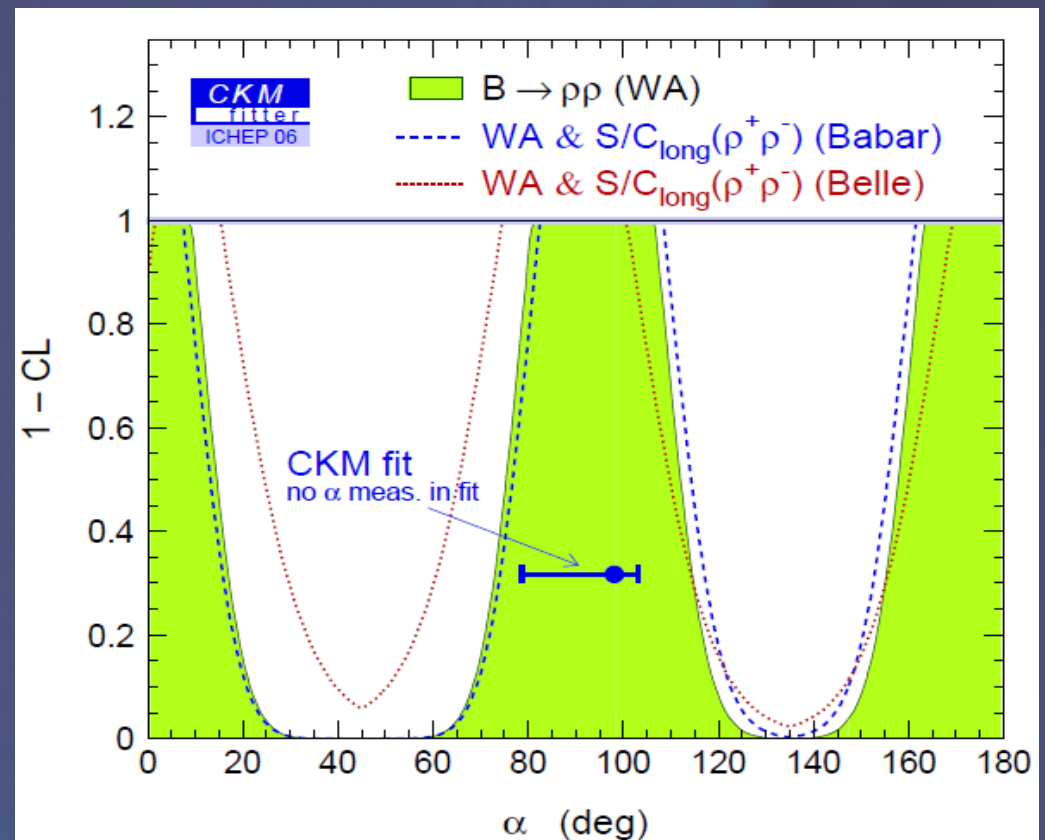
# Measurement of $\phi_2$

## EPS'2005 Result



The constraint become less stringent.  
(The isospin triangle now closed with new  $\rho^+\rho^0$  branching fraction.)

## ICHEP'2006 Result



## New Inputs:

$$BR(B \rightarrow \rho^+ \rho^-) = 23.1^{+3.1}_{-3.2} \times 10^{-6}$$

$$BR(B \rightarrow \rho^+ \rho^0) = 18.2 \pm 3.0 \times 10^{-6}$$

$$A_{CP}(B \rightarrow \rho^+ \rho^0) = -0.08 \pm 0.13$$

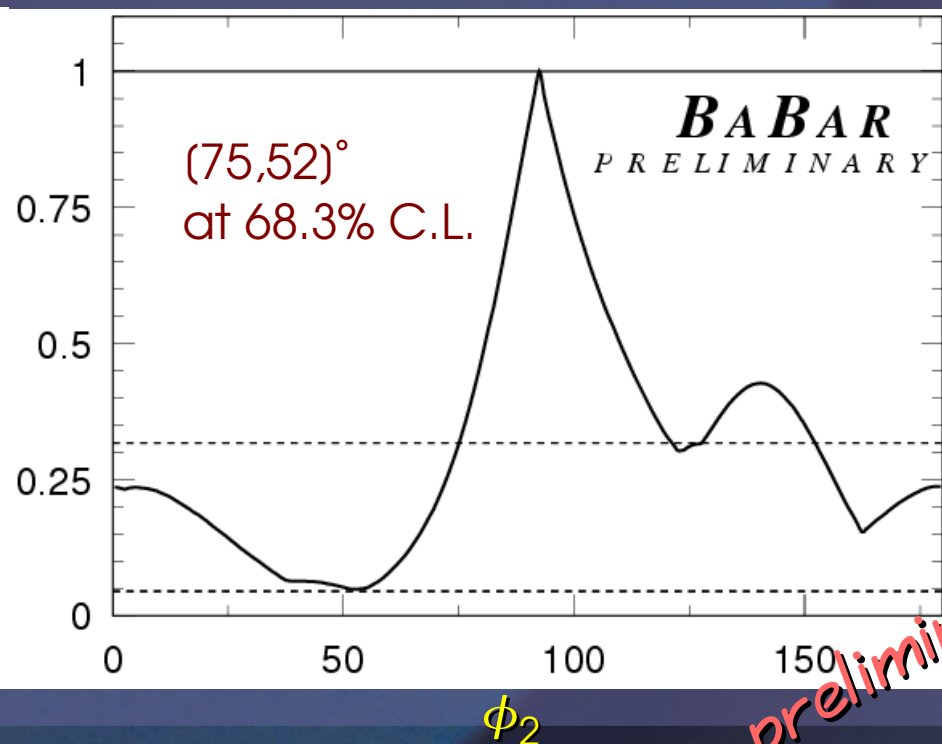
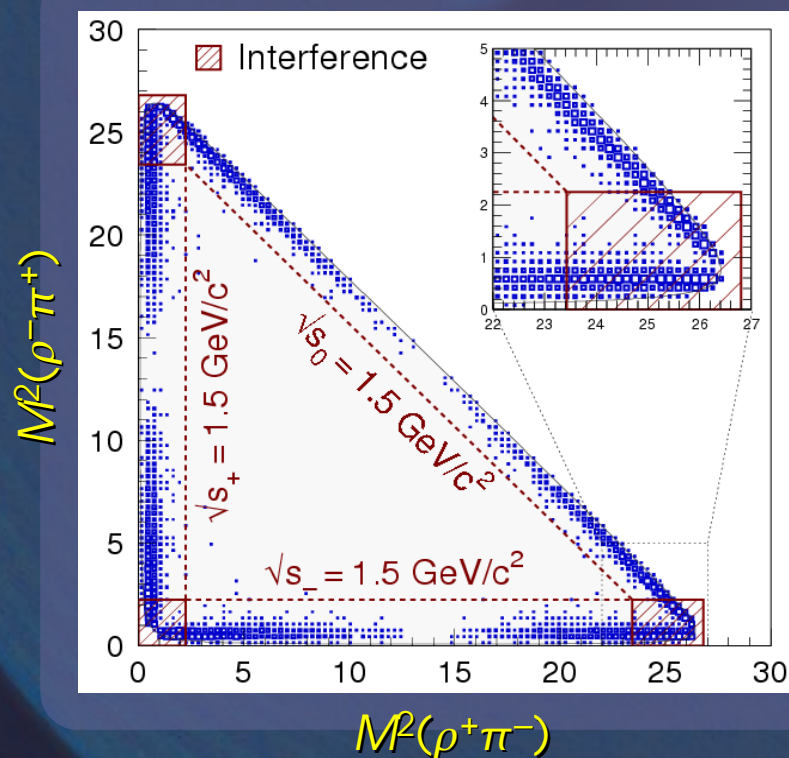
$$BR(B \rightarrow \rho^0 \rho^0) = 1.2 \pm 0.5 \times 10^{-6}$$

# TCPV + Dalitz in $B \rightarrow \rho\pi$



347M  $BB$  pairs

Time-dependent Dalitz-plot analysis assuming isospin symmetry,  
measuring 26 coefficients of the bilinear form factors  
(A.Snyder, H. Quinn, Phys. Rev. D, 48, 2139 (1993))

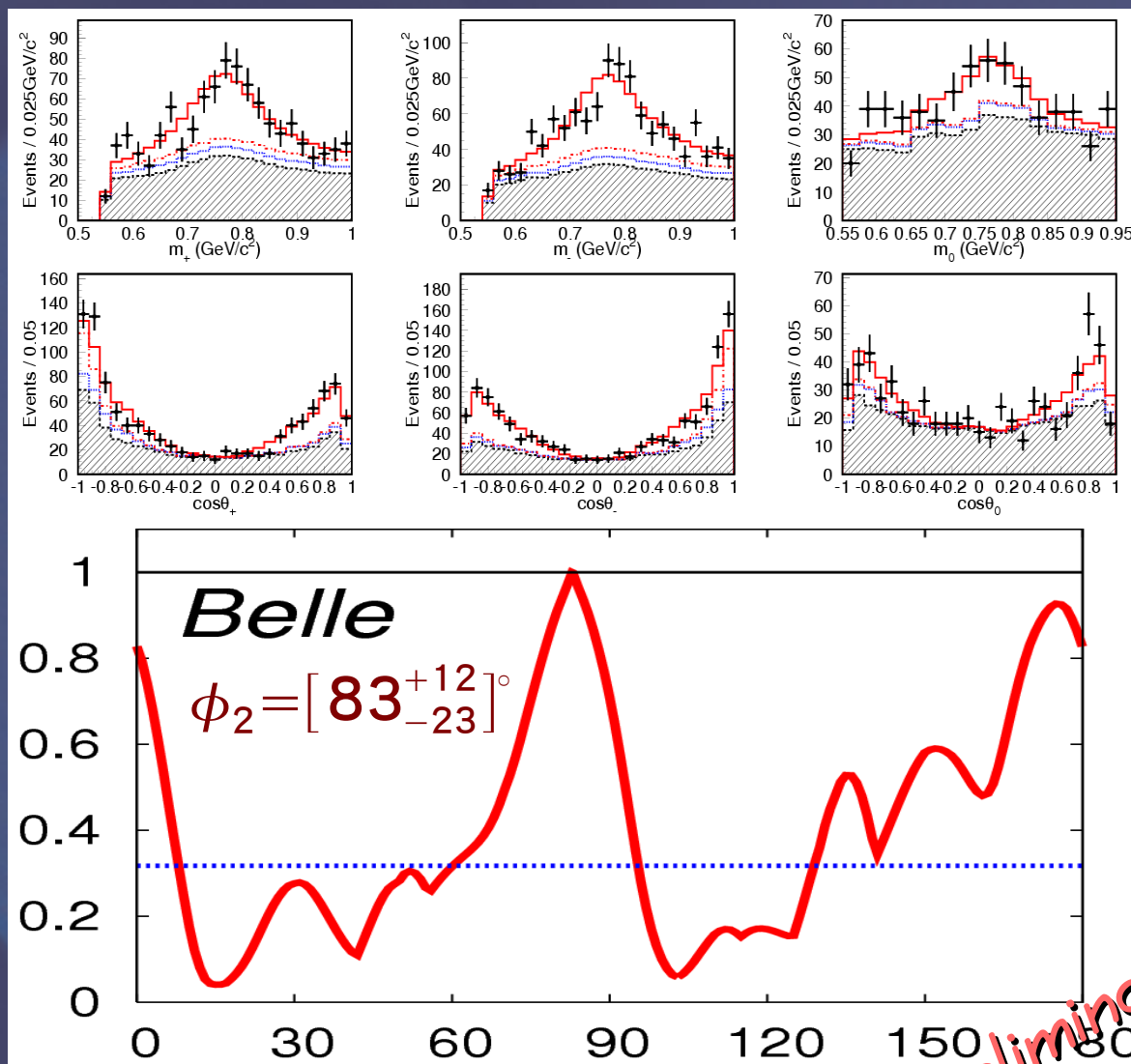
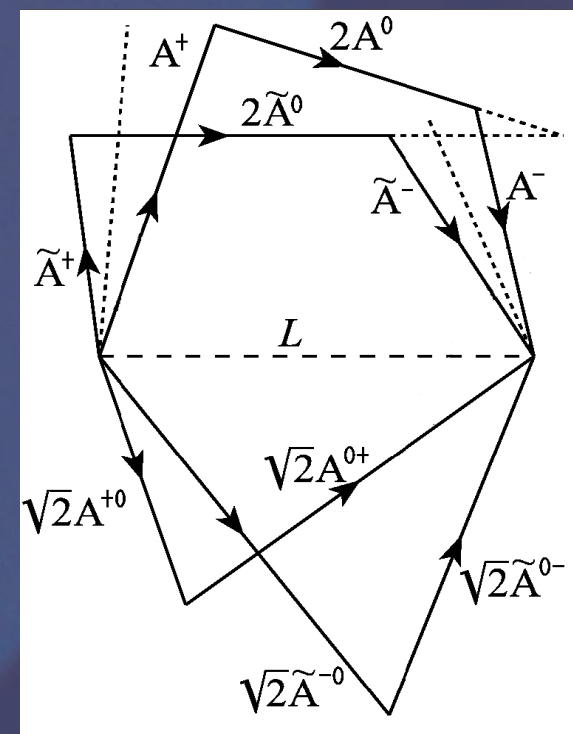


# TCPV + Dalitz in $B \rightarrow \rho\pi$



447M  $BB$  pairs

- Time-dependent Dalitz analysis + isospin (pentagon) analysis ↗

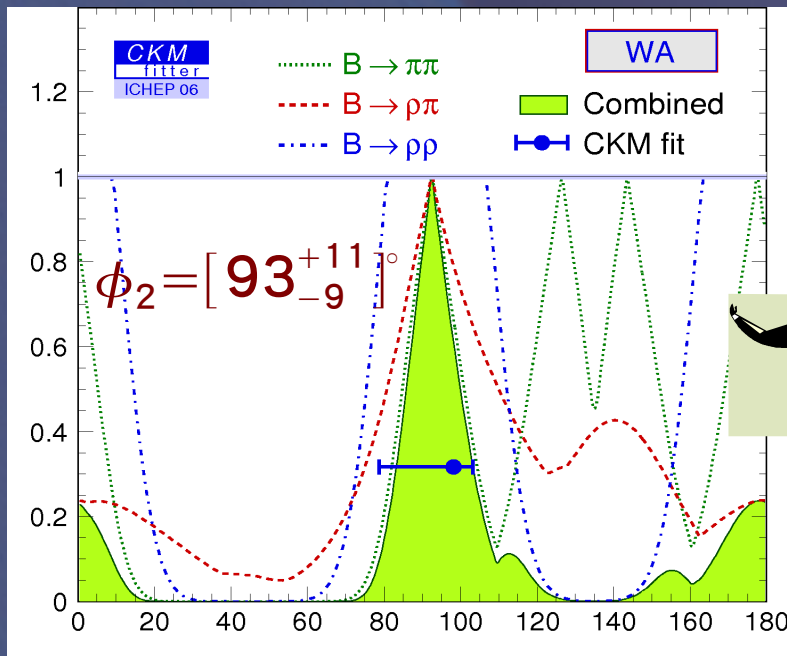




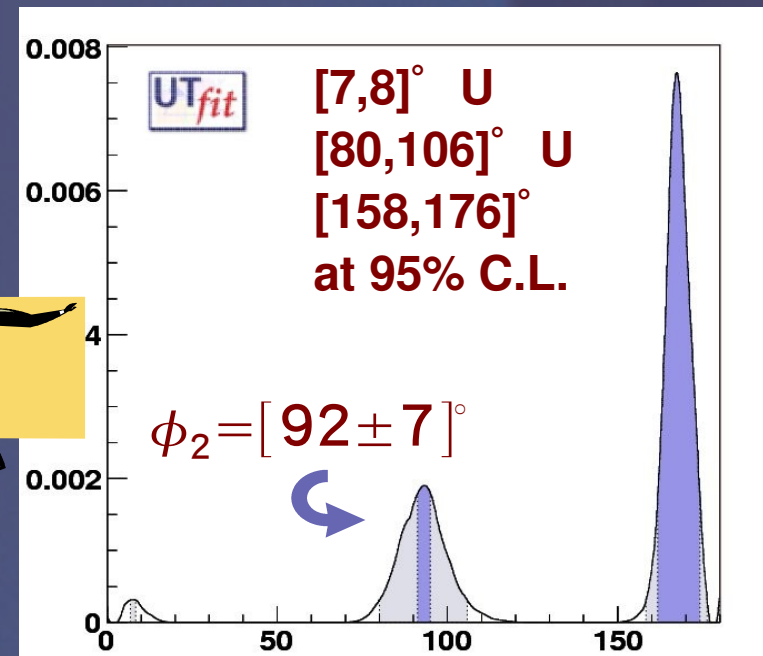
# $\phi_2$ World Average

Averages from BaBar's  $\pi\pi/\rho\rho/\rho\pi$  and Belle's  $\pi\pi/\rho\rho$  [ $\rho\pi$ ]:

CKMFitter



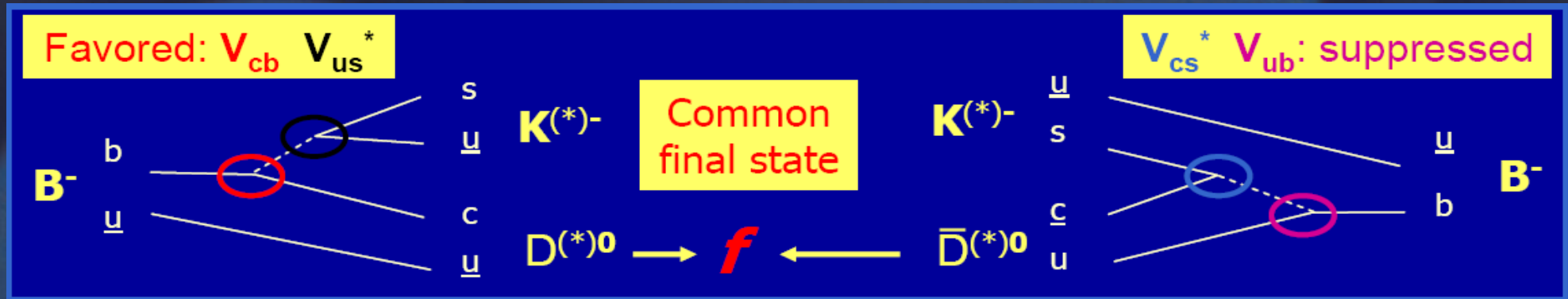
UTFit



- Unmatched CKMFitter & UFit results.
- Ambiguity @ 90 or 180 degrees ( $\rho\pi$  is sensitive to this issue).
- Need to include Belle's  $\rho\pi$  result for CKMFitter.

# Measurement of $\phi_3$

Interference between  $B \rightarrow DK$  and  $B \rightarrow \bar{D}K$  :



$$A\left(\frac{B^- \rightarrow \bar{D}^0 K^-}{B^- \rightarrow D^0 K^-}\right) = \boxed{r_B} \cdot \exp(i \boxed{\delta_B}) \cdot \exp(-i \boxed{\phi_3})$$

Mode-by-mode para.      Common CKM angle

Three methods for exploiting interference (choice of  $D^0$  decay modes):

- Gronau, London, Wyler (GLW): Use CP eigenstates of  $D^{(*)0}$  decay, e.g.  $D^0 \rightarrow K_S \pi^0$ ,  $D^0 \rightarrow \pi^+ \pi^-$
- Atwood, Dunietz, Soni (ADS): Use doubly Cabibbo-suppressed decays, e.g.  $D^0 \rightarrow K^+ \pi^-$
- Giri, Grossman, Soffer, Zupan (GGSZ) / Belle: Use Dalitz plot analysis of 3-body  $D^0$  decays, e.g.  $K_S \pi^+ \pi^-$

Updated  
on ICHEP'06

# Dalitz Analysis

- Measure the  $B^+/B^-$  asymmetry across the Dalitz plot.
- Extract the CKM angle  $\phi_3$  from the interference term:

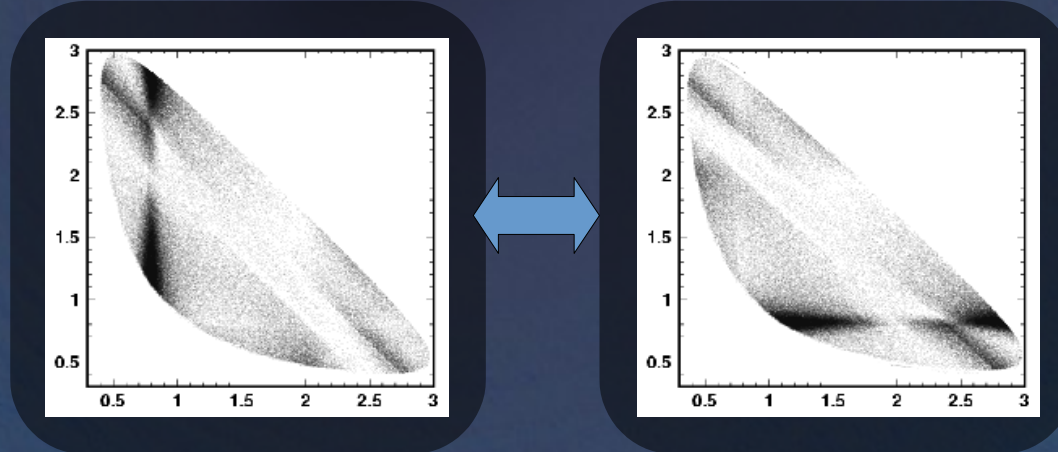
Decay:

$$B^\pm \rightarrow [K_S \pi^+ \pi^-]_D K^\pm$$

Amplitudes:

$$A^\pm = f(m_+^2, m_-^2) + r_B \exp(\pm i\phi_3) \exp(i\delta_B) f(m_-^2, m_+^2)$$

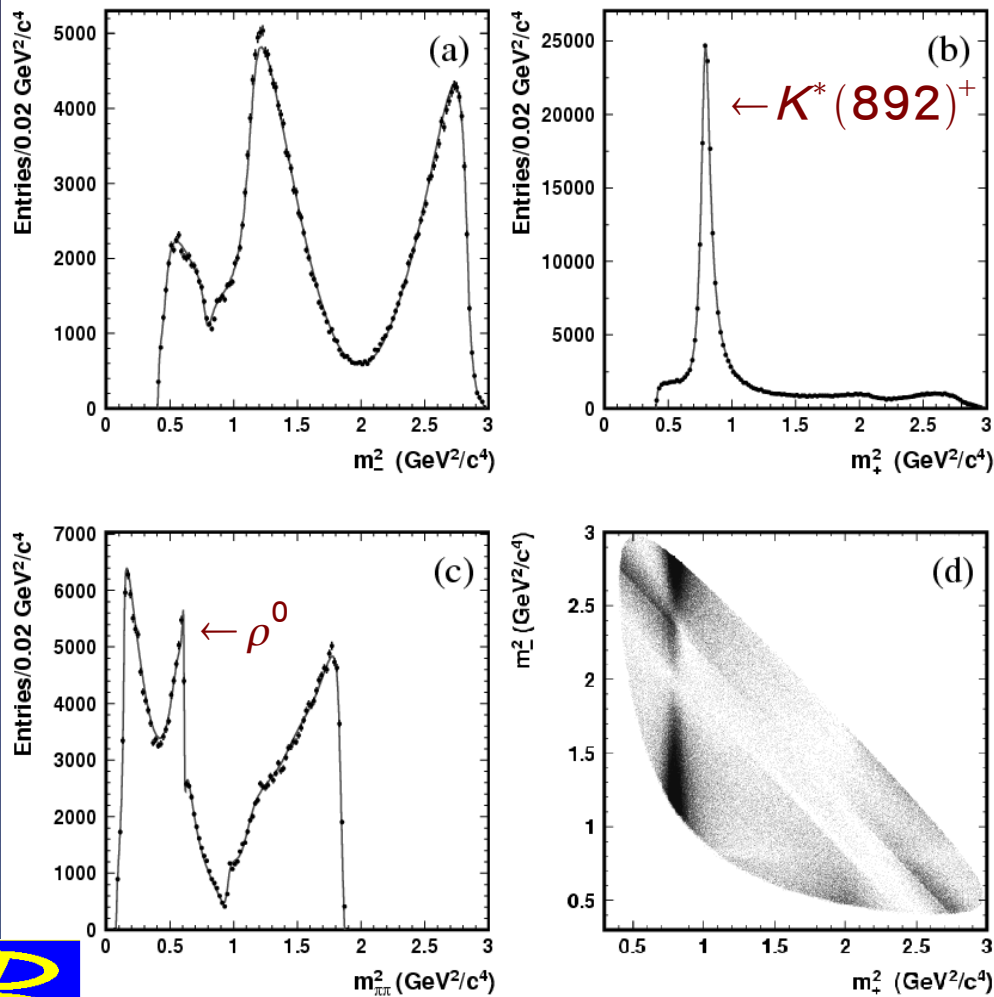
$$[m_\pm = m(K_S, \pi^\pm)]$$



- Also covers GLW ( $D^0 \rightarrow K_S \rho^0$ ,  $CP$ -eigenstate) and ADS ( $D^0 \rightarrow K^{*+} \pi^-$ , DCS 2-body decay) regions.
- A 2-fold ambiguity on  $\phi_3$ :  $(\phi_3, \delta) \rightarrow (\phi_3 + \pi, \delta + \pi)$



# Dalitz Modeling



- Select  $D^{*+} \rightarrow [K_S \pi^+ \pi^-] \pi^+$  events.
- Fit to a set of 18 2-body amplitudes and a non-resonant component:

$$f(m_+^2, m_-^2) = \sum_{j=1}^N a_j e^{i\alpha_j} A_j(m_+^2, m_-^2) + b e^{i\beta}$$

- Main contributions from:

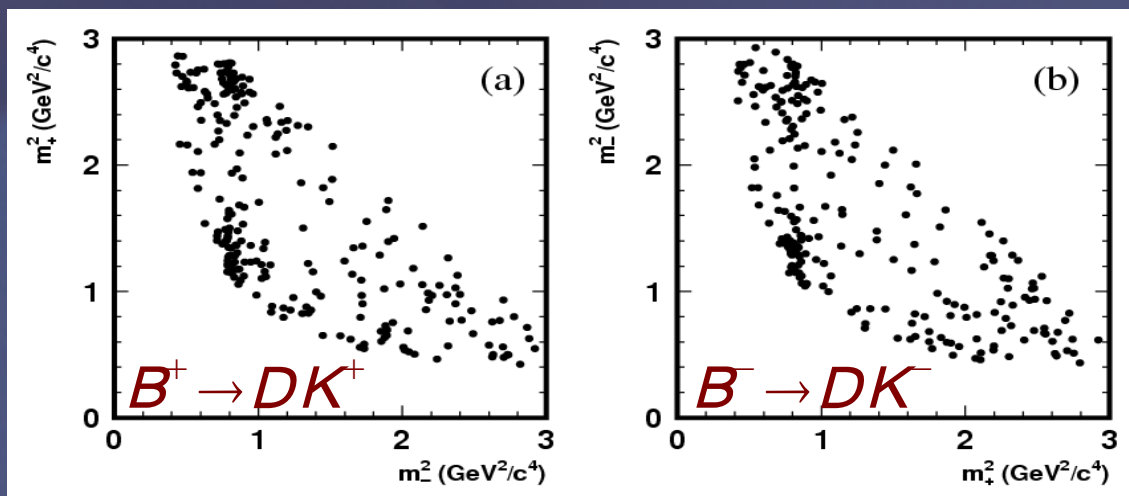
$$D \rightarrow K^*(892)^+ \pi^-$$

$$D \rightarrow K^*(1430)^+ \pi^-$$

$$D \rightarrow K_S \rho^0$$



# Dalitz Plots from $B \rightarrow DK$



$$N(B^+ \rightarrow D^0 K^+) = 331 \pm 23$$

$$N(B^+ \rightarrow D^{*0} K^+) = 81 \pm 11$$

$$N(B^+ \rightarrow D^0 K^{*+}) = 54 \pm 8$$



386M BB

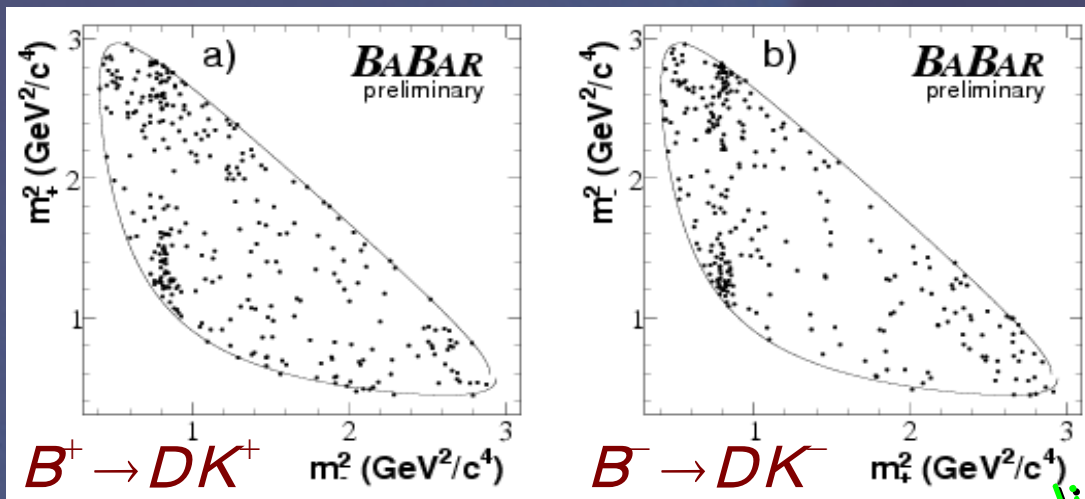


347M BB

$$N(B^+ \rightarrow D^0 K^+) = 398 \pm 23$$

$$N(B^+ \rightarrow D^{*0} K^+) = 190 \pm 18$$

$(D^{*0} \rightarrow D^0 \pi^0, D^0 \gamma)$

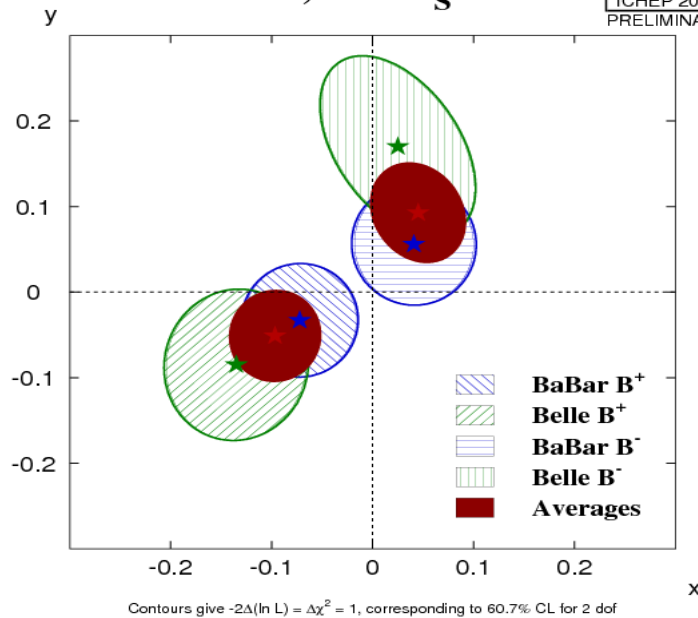


preliminary

\* w/o Dalitz modeling error

$DK^+, D \rightarrow K_S \pi^+ \pi^-$

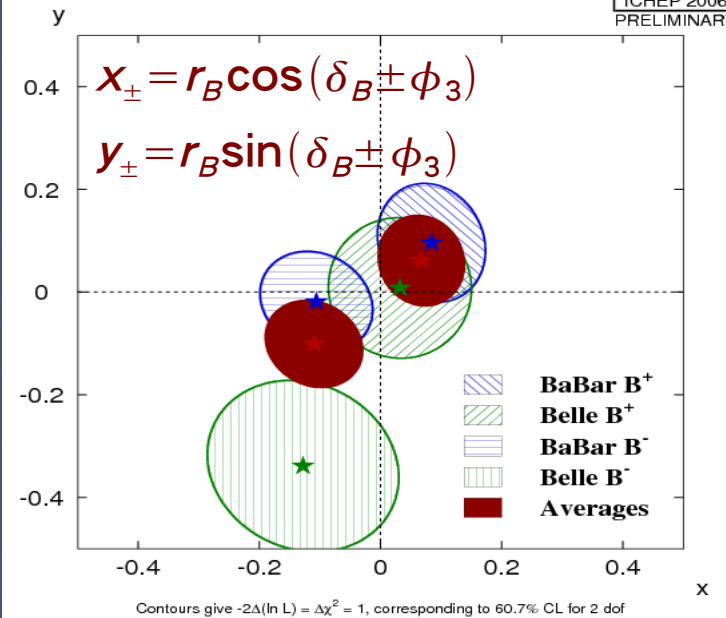
HFAF  
ICHEP 2006  
PRELIMINARY



\* w/o Dalitz modeling error

$D^* K^+, D^* \rightarrow D\pi^0 \& D\gamma, D \rightarrow K_S \pi^+ \pi^-$

HFAF  
ICHEP 2006  
PRELIMINARY



□ Measurement on  $\phi_3$ :



$$\phi_3 = (53^{+15}_{-18} \pm 3 \pm 9)^\circ$$

$(B^\pm \rightarrow D^0 K^\pm, D^{*0} K^\pm, D^0 K^{*\pm})$



$$\phi_3 = (92 \pm 41 \pm 11 \pm 12)^\circ$$

$(B^\pm \rightarrow D^0 K^\pm, D^{*0} K^\pm)$

preliminary

(The result which is consistent with SM fit is quoted here.)

CKMFitter or UFit is required for Belle/BaBar average.



# Summary

$$\phi_1/\beta$$

- ❑ The standard " $\sin 2\phi_1$ " has been measured very well.
- ❑ New target – " $\sin 2\phi_1$ " with  $b \rightarrow s$  penguins will be examined with more data.

$$\phi_2/\alpha$$

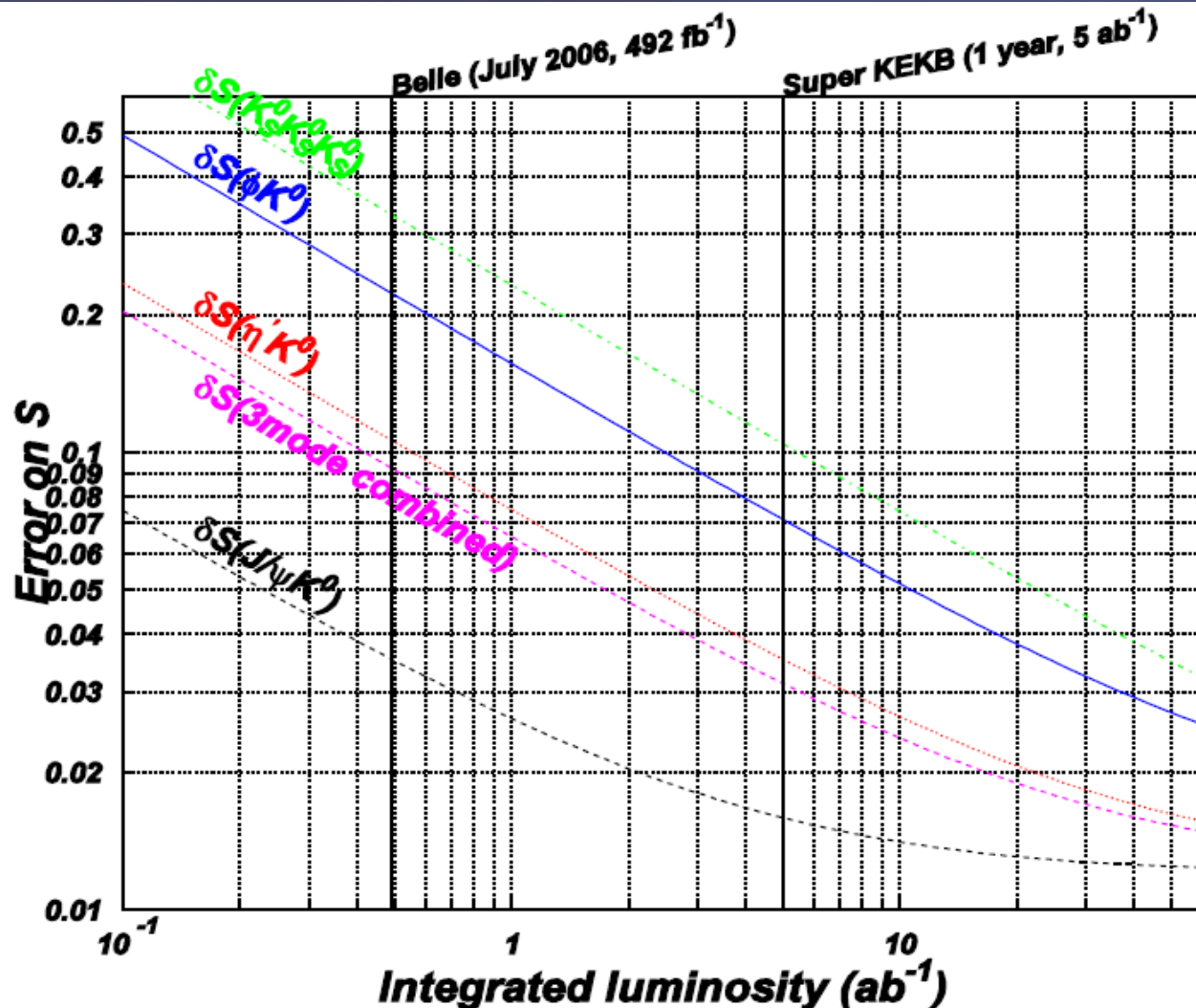
- ❑ The angle has been measured with several decay modes.
- ❑ The discrepancy between 2 experiments has not been 100% solved – more data is required.
- ❑ Need to understand how to include the  $\rho\pi$  data in the UT/CKM fitters.

$$\phi_3/\gamma$$

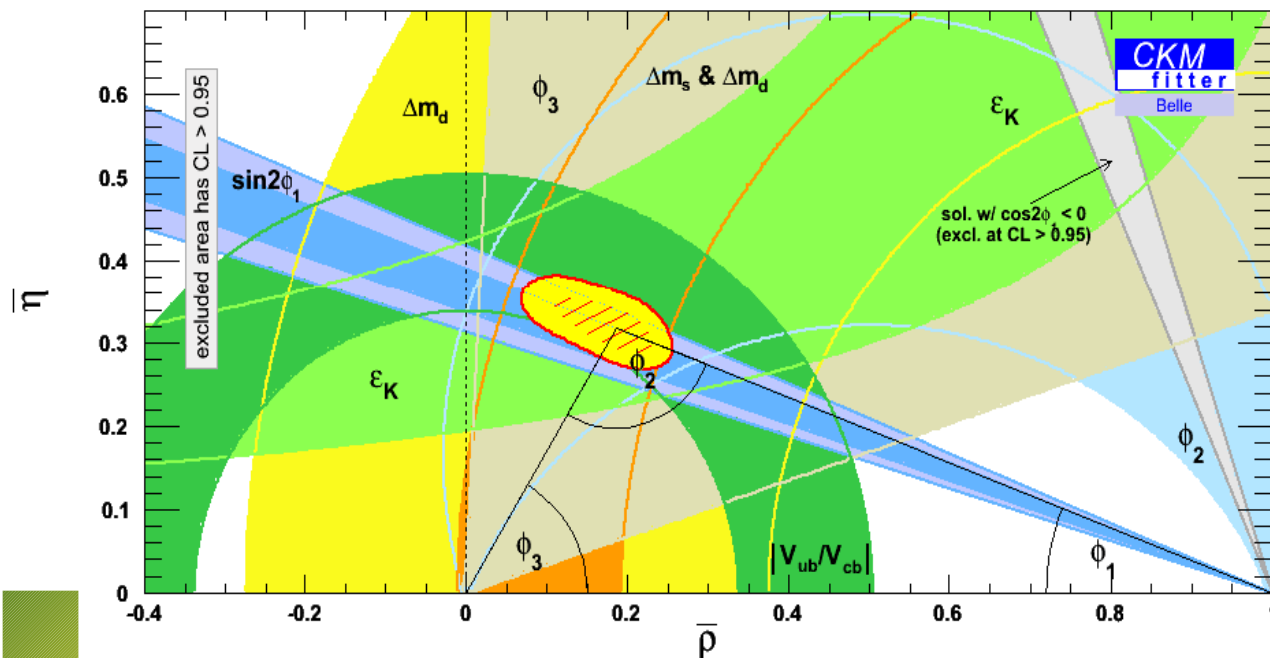
- ❑ The  $\phi_3$  angle is measured by 2 groups with different assumptions.
- ❑ No average result can be made unless an unification of analysis methods being made.

➡ A little bit on the future prospects?

# Prospects on $\delta S$



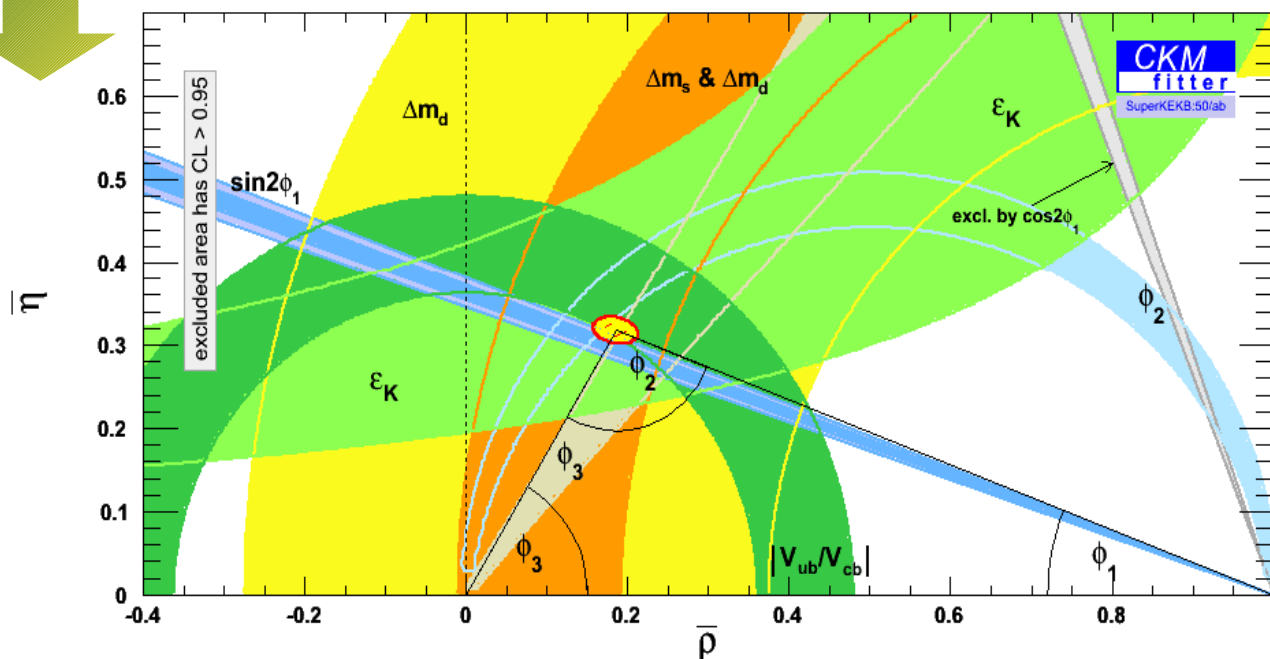
- Expected error on  $\sin 2\phi_1$ :  
 $0.016 @ 5/\text{ab}$   
 $0.012 @ 50/\text{ab}$
- Limited by vertexing systematic errors



Belle w/ 0.5/ab  
(current data)

$$\delta\phi_2 \sim 11^\circ$$

$$\delta\phi_3 \sim 15^\circ$$

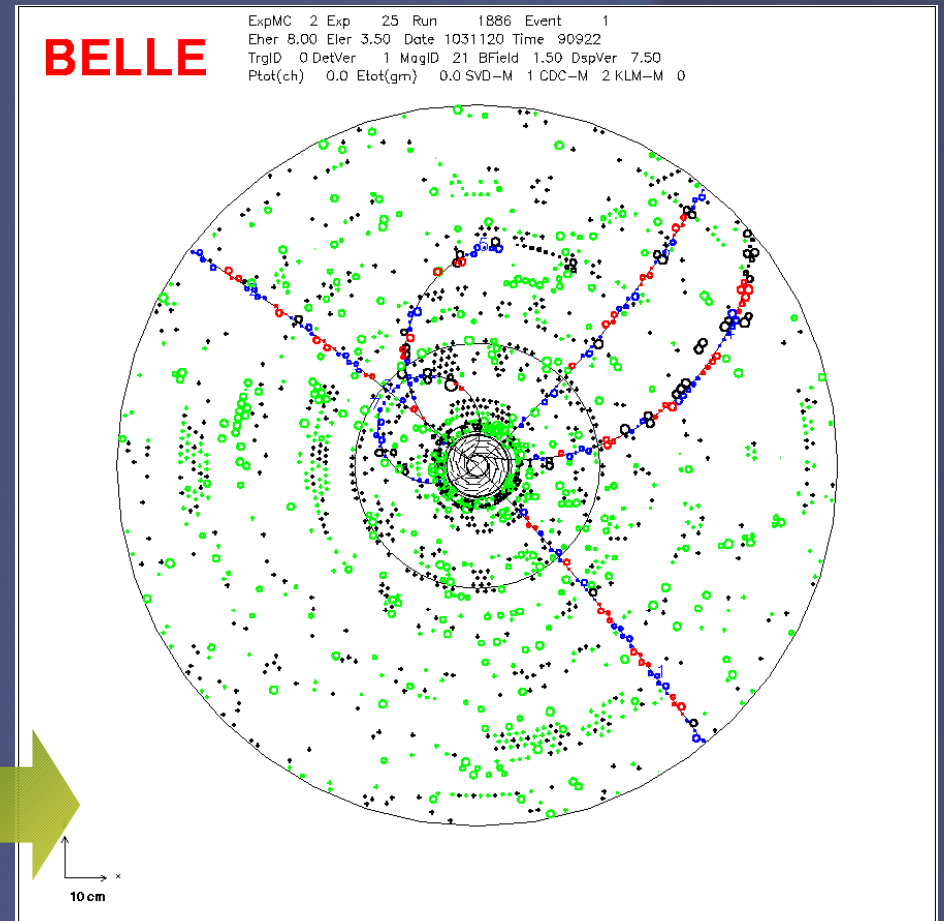
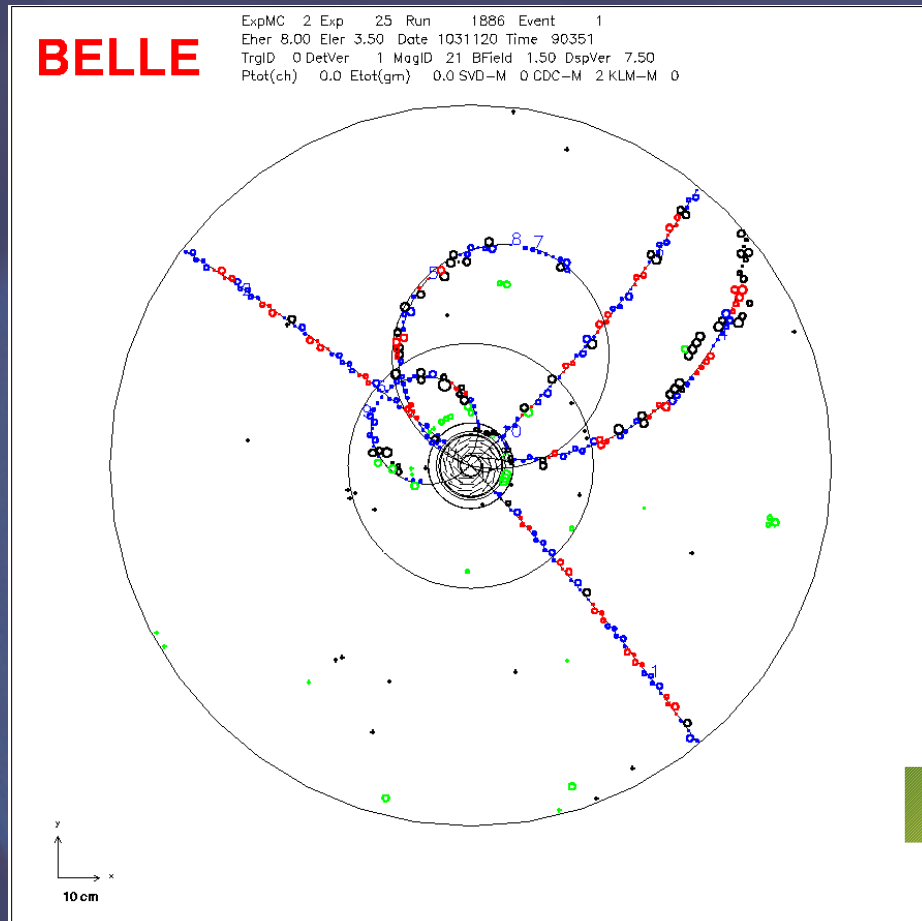


Belle w/ 50/ab

$$\delta\phi_2 \sim 2^\circ$$

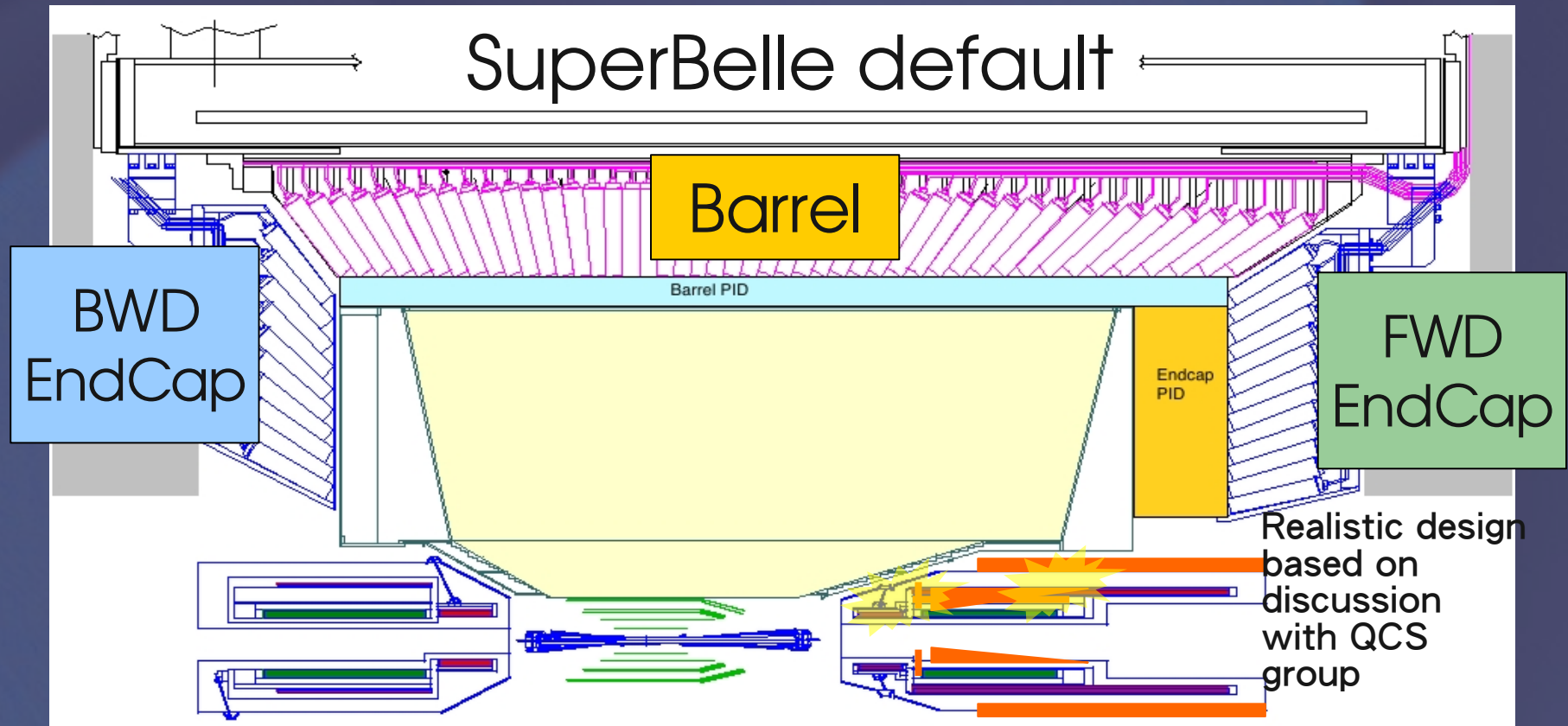


# Challenge for the Exp.



The expected beam background will be also 20x larger!

# Super *B* Detector



Vertex: Si triplet inner-most and Si strip tracker

Tracker: Drift chamber  $r > 15\text{cm}$

PID: w/TOP and AC-RICH (endcap)

ECAL: CsI (TI) + wave from (barrel) pure CsI+PMT (endcap)





Tsukuba?



Super *B* Return?



Frascati?